Dear Editor:

Thank you for your letter dated December 12 regarding our manuscript entitled “Could the mesoscale eddies be reproduced and predicted in the northern south China sea: case studies” (No: os-2018-74), which was submitted to Ocean Science for consideration of publication. We have read reviewer’s comments carefully. Following your suggestions, we have gone through the manuscript and made the following changes in the manuscript.

The line-by-line replies for reviewer’s comments are shown in the attachments. The original comments are quoted in Times New Roman (Bold) and our responses are in Times New Roman.

Once again, thank you and reviewer for the time and energy spending on reading our manuscript and providing constructive comments and suggestions, which are very valuable in improving the quality of our manuscript.

Enclosed, please find our updated manuscript and reply to the reviewer’s comments.

We hope this version of our manuscript can meet the standard of publication in this journal, and we look forward to receiving further instruction related to this submission.

Sincerely yours

Dazhi Xu
Dear Authors

Thank-you for your revisions. I think some of the review comments are “open to interpretation” and so am still asking for some “Minor Revision”. This is for clarity and to include more of what I think the reviewers were asking for. My comments follow here.

**Ans:** We are very grateful to the editor for the recognition of our work, and we are very grateful for your efforts and time to improve the quality of this article.

**Comments**

**Page 3**

**Lines 31-32. Better “...atmosphere, ocean mesoscale eddies are often described...”**

**Ans:** Thank you. The sentences have been revised in the revised version. (P3, line 31-32)

**Lines 39-40. You have added the references but I think Referee 1 wanted a few words about what is learned from these references, e.g. scales resolved (Fu et al), eddy energy and tracking (Morrow and Le Traon), effects on atmosphere (Frenger et al.).**

**Ans:** Thank you for your constructive advice. The sentences have been rewrote to adapt to the added references in the revised version. (P3, line 45-47)

**Line 42 (or nearby). I am sure Referee 2 comment 2 wants more text about motivation in your manuscript, not just the references. Their comment is a suggestion for what to include.**

**Ans:** Thank you. These contents have been added in the revised version. (P3, line 37-45)

**Page 3 line 51 to Page 4 line 1. Better “...exhibits significant mesoscale eddy activity (Fig. 2). Many studies have tried to investigate mesoscale eddies in the NSCS...”**

**Ans:** Thank you. The sentences have been revised in the revised version. (P4, line 61-62)
Page 4

Line 57. “. . recorded evidence . .” (omit “the”)
Ans: Thank you. The word “the” has been deleted in the revised version. (P4, line 67)

Ans: Thank you. The sentences have been revised in the revised version. (P5, line 82)

Line 73. “. . disappeared southeast of Hainan . .”
Ans: Thank you. The sentences have been revised in the revised version. (P5, line 83)

Page 5

Lines 78-79. “. . Despite the activities . . NSCS having received . .”
Ans: Thank you. The sentences have been revised in the revised version. (P5, line 87-88)

Line 82. “. . (Oey et al., 2005); they are . .”
Ans: Thank you. The sentences have been revised in the revised version. (P5, line 91)

Line 87. You have added the references suggested by Referee 1. However, I think you also need to comment on what they show (achieve), what is still needed and so how your study helps.
Ans: Thank you. The contents have been added in the revised version. (P6, line 96-103)

Line 88. “. . two typical anticyclonic eddies . .” Are these AE1 and AE2 (not clear as you have re-arranged the text)? Referee 1 (main comment 1) asked why these two particular eddies were chosen; you should say (they ought to be representative, survive long enough to be useful . . . etc.).
Ans: Thank you. The contents have been added in the revised version. (P6, line 104-105)

Page 6

Line 112. “. . System, are also used. . .” It would be better to divide this sentence which is too long.
Ans: Thank you. The sentence has been revised in the revised version. (P7, line 129)

Line 116. “. . used. Three drifters were designed”
Ans: Thank you. The sentence has been revised in the revised version. (P7, line 133-134)
Lines 122-126. “. . study as follows: 1) there must be a closed contour on the merged SLA; 2) there must be one maximum or minimum inside the area of the closed contour for anticyclonic or cyclonic eddy; 3) the difference between the extremum and the outermost closed SLA contour, that is, the amplitude of the mesoscale eddy, must be greater than 2 cm; . ."

**Ans:** Thank you. The sentences have been revised in the revised version. (P8, line 140-144)

Line 136. “weak” -> “weakly”

**Ans:** Thank you. The word “weak” has been changed to “weakly” in the revised version. (P8, line 153)


**Ans:** Thank you. The expression of the reference has been corrected in the revised version. (P9, line 173-174)

Page 9

Line 176. Please check fonts and alignment for “a”, “b”, “d”.

**Ans:** Thank you. All formulas and symbols have been rewritten and corrected in the revised version. (P10, line 191-P11, line 205)

Line 179. Likewise fonts for P, R to match symbols in equation (2).

**Ans:** Thank you. All formulas and symbols have been rewritten and corrected in the revised version. (P10, line 190-P11, line 204)

Page 10.

Line 190. “. . CSCASS are in Li . .”

**Ans:** Thank you. The sentence has been revised in the revised version. (P11, line 207)

Line 193. “. . reproduction of anticyclonic eddies AE1 and AE2 in the NSCS . .”

**Ans:** Thank you. The section topic has been revised in the revised version. (P11, line 211)

Lines 197-198. “. . into CSCASS every 3 days . .”

**Ans:** Thank you. The sentence has been revised in the revised version. (P11, line 214)

Page 11.
Line 209. “. . when the ANP is greater . .”

*Ans:* Thank you. The sentence has been revised in the revised version. (P12, line 226)

Lines (209-210). “. . when the ANP is greater than 2 (that is the amplitude greater than 8 cm) . .” These two criteria are not the same thing. It is possible for ANP < 2 but amplitude > 8 cm for a large eddy.

*Ans:* Thank you. The sentence has been revised in the revised version (P12, line 226). We fully agree with you. But, as our research shown, the ANP > 2 and the amplitude > 8cm is corresponding. As for the existence of the phenomenon you mentioned, more researches are needed to verify it and we will strengthen this research in subsequent investigation.

Line 210. “well reproduced”. Referee 1 main comment 3 asks for an objective measure for good reproduction. Please say how you measure it.

*Ans:* Thank you. In this study, we can only be qualitative, cannot quantitatively determine the quality of reproduction. As for the criterion, we mainly judge whether the eddy center distance and the amplitude change trend are consistent between the observed and the assimilation results.

Line 218. “. . CSCASS: the meridional and zonal radii of AE1 . .”

*Ans:* Thank you. The sentence has been revised in the revised version. (P12, line 235)

Lines 223-224. “. . (Fig. 7b-7j), e.g. moving northwestward firstly and then southwestward, can generally . .”

*Ans:* Thank you. The sentence has been revised in the revised version. (P12, line 240-241)

Page 12.

Line 230. “. . their observed amplitude”

*Ans:* Thank you. The sentence has been revised in the revised version. (P13, line 248-249)

Line 232. “relatively small, less than 8 cm, . .”. But this criterion “8 cm” may depend on altimeter accuracy (Referee 1 main comment 2). You should discuss how the criterion might differ in other contexts. Most readers will not be repeating your work in the NSCS but may want to know a criterion in their context.

*Ans:* Thank you. The sentence has been revised in the revised version (P13, line 249). Yes, the criterion “8 cm” is relating with the SLA error of assimilation system. For
example, the mean SLA error of the CSCASS in the SCS is about 8cm.

Line 235. “assimilated . .”

**Ans:** Thank you. The word “assimilating” has been changed to “assimilated” in the revised version. (P13, line 252)

Page 13.


**Ans:** Thank you. The year “2003” has been changed to “2004” in the revised version. (P14, line 270)

Line 255. “disappearance”

**Ans:** Thank you. The word “disappear” has been changed to “disappearance” in the revised version. (P14, line 272)

Page 14.

Line 273. “. . and then enhancement of AE1 was also predicted . .”

**Ans:** Thank you. The sentence has been revised in the revised version. (P14, line 290)

Line 278. Delete “which”.

**Ans:** Thank you. The word “which” has been deleted in the revised version. (P15, line 295)

Line 279. “continued”

**Ans:** Thank you. The word “continue” has been changed to “continued” in the revised version. (P15, line 296)

Line 284. “reproduce . .”

**Ans:** Thank you. The word “reproduced” has been changed to “reproduce” in the revised version. (P15, line 300)

Line 287. “. . but the predicted movement is firstly toward . .”

**Ans:** Thank you. The sentence has been revised in the revised version. (P15, line 304)

Page 15.

Line 296. “slow”

**Ans:** Thank you. The word “slowly” has been changed to “slow” in the revised version. (P15, line 313)
Line 309. “. . and movement direction . .”

**Ans:** Thank you. The word “moving” has been changed to “movement” in the revised version. (P16, line 325)

Lines 310-311. “. . AE2 are keeping in the consistent trend (Fig. 14e) . .”. This is very unclear. Also the figure does not show much consistency between the observed amplitude (overall decrease) and predicted amplitude (overall increase), but the observed and predicted amplitudes are getting closer with time.

**Ans:** Thank you. The sentence has been revised in the revised version. (P16, line 327-328)

Page 16.

Line 316. “owing to the low amplitude . .”

**Ans:** Thank you. The sentence has been revised in the revised version. (P16, line 333)

Line 325. “. . production and predictability . .”

**Ans:** Thank you. The word “productivity” has been changed to “production” in the revised version. (P17, line 342)

Lines 327-328. Better “. . The comparisons of AE1 and AE2 observations with CSCASS prediction experiments, which assimilate SLA and SST, show that . .”?

**Ans:** Thank you. The sentence has been revised in the revised version. (P17, line 344-345)

Line 331. “disappearance”. Again there is the question of what uncertainty determines the value 8 cm.

**Ans:** Thank you. As our result shows, the SLA error of assimilation system determines the value 8 cm.

Lines 333-334. “. . prediction experiments . . with observations . .”

**Ans:** Thank you. The sentence has been revised in the revised version. (P17, line 350-351)

Page 17.

Line 336. “generation”

**Ans:** Thank you. The word “generative” has been changed to “generation” in the revised version. (P17, line 353)

Lines 341-342. “. . reproduction and predictability. As . .”
Thank you. The sentence has been revised in the revised version. (P18, line 358)

Lines 348-350. Better “it cannot make up for limitations of numerical model algorithms and resolution. Hence for high-resolution operational oceanography, numerical models . .”

Thank you. The sentences have been revised in the revised version. (P18, line 364-366)

Page 20 lines 404-407. These two references should be in reversed order.

Thank you. The order of the two references has been corrected in the revised version. (P21, line 421-424)
Could the two anticyclonic eddies during winter 2003/2004 be reproduced and predicted in the northern South China Sea?

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Abstract

Great progress has been made in understanding the mesoscale eddies and their role on the large-scale structure and circulation of the oceans. However, many questions still remain to be resolved, especially with regard to the reproducitivity and predictability of mesoscale eddies. In this study, the reproducitivity and predictability of mesoscale eddies in the Northern SCS (NSCS), a region with strong eddy activity, are investigated with a focus on two typical anticyclonic eddies (AE1 and AE2) based on a HYCOM-EnOI Assimilated System. The comparisons of assimilated results and observations suggest that generation, evolution and propagation paths of AE1 and AE2 can be well reproduced and forecasted when the observed amplitude >8 cm (or the advective nonlinearity parameter U/c greater than 2), although their forcing mechanisms are quite different. However, when their amplitudes are less than 8 cm, the generation and decay of these two mesoscale eddies cannot be well reproduced and predicted by the system. This result suggests, in addition to dynamical mechanisms, the spatial resolution of assimilation observation data and numerical models must be taken into account in reproducing and predicting mesoscale eddies in the NSCS.

Keywords: HYCOM; EnOI; Northern South China Sea; Mesoscale eddy; Predictability
1. Introduction

Equivalent to the synoptic variability of the atmosphere, the ocean mesoscale eddies are often described as the “weather” of the ocean, with typical spatial scales of ~100 km and time scales of a month (Wang et al., 1996; Liu et al., 2001; Chelton et al., 2011). The mesoscale eddy is characterized by temperature and salinity anomalies with associated flow anomalies, exhibiting different properties to their surroundings, thus allowing them to control the strength of mean currents and to transport heat, salt, and biogeochemical tracers around the ocean. The motion of mesoscale eddies would be a straight line, if eddies freely propagate in open ocean. However, most of eddies may have interaction with topography, strong currents (western boundary current), eddies during their lifetime. The motion of eddy will be modified and even split when approaching an island (Yang et al., 2017). It is also recognized that western boundary is graveyard of eddies (Zhai et al., 2010). The dynamical processes such as splitting and/or merging of eddies can also make termination and/or genesis of eddies in open ocean (Li et al., 2016). Thus, the dynamical processes make that the prediction of eddy motion is a challenge for ocean simulation. Although today, the beauty and complexity of the scales resolved, the eddy energy and tracking and the effects on atmosphere of these mesoscale features can be seen by viewing high resolution satellite images or numerical model simulations (Yang et al., 2000; Fu et al., 2010; Morrow and Le Traon, 2012; Frenger et al., 2013), the operational forecasts of the mesoscale eddy still pose a big challenge because of its complicated dynamical mechanisms and high nonlinearity (Woodham et al., 2015; Treguer et al., 2017; Vos et al., 2018). A recent example is the
explosion of the Deepwater Horizon drilling platform in the northern Gulf of Mexico in 2010 where an accurate prediction of the position and propagation of the Loop Current eddy was essential in determining if the spilled oil would be advected to the Atlantic Ocean or still remain within the Gulf (Treguier et al., 2017).

Similar to Gulf of Mexico, the South China Sea (SCS) is also a large semi-closed marginal sea in the northwest Pacific, connecting to the western Pacific through the Luzon Strait (Fig. 1). Forc ed by seasonal monsoon winds, the intrusion of Kuroshio Current (KC), the Rossby waves and the complex topography, the SCS, especially the Northern SCS (NSCS) exhibits a significantly high mesoscale eddy activity (Fig. 2). Many studies have tried to investigate the mesoscale eddies in the NSCS (Wang et al., 2003; Jia et al., 2005; Wang et al., 2008). Based on the potential vorticity conservation equation and in-situ survey data, Yuan and Wang (1986) pointed out that the bottom topography forcing might be the primary factor for the formation of anticyclonic eddies in the northeast of Dongsha Islands (DIs). Using survey CTD data in September 1994, Li et al. (1998) recorded the evidence of anticyclonic eddies in the NSCS and suggested these anticyclonic eddies are probably shed from the KC. Investigations by Wu et al. (2007) showed that westward propagating eddies in the NSCS originate near the Luzon Strait rather than coming from the western Pacific. Based on the altimeter, the trajectory of drift and the hydrological observations data, Wang et al. (2008) studied the evolution and migration of two anticyclonic eddies in the NSCS during winter of 2003/2004. As they described, the AE1 generated by interaction of the unstable rotating fluid with the sharp topography of DIs firstly
appeared near DIs on the 10th of December 2003 (see Fig. 3). Then it began to move
southwestward with its amplitude decreasing gradually. During the movement of AE1, another anticyclonic eddy (AE2) was shed and developed from the loop current of
Kuroshio near the Luzon Strait on the 14th of January 2004. The amplitude of AE2 was
then increased when it propagated southwestward (Fig. 3d-3f). About five weeks later, AE2 reached its maximum in amplitude and then lasted around three weeks in its mature state. During its decay phase, AE2 moved southwestward quickly with its amplitude decreasing, and finally disappeared at the location of 114°E, 18°N on the 7th of April 2004. Meanwhile, AE1 continued moving to southwest and eventually disappeared in the southeastern of Hainan. In addition to physical characteristics, the phytoplankton community at these two eddies have also been studied by Huang et al. (2010). These studies improved our understanding of activities of mesoscale eddy and its possible dynamical mechanisms in the NSCS.

Despite the studies on the activities and its possible dynamical mechanisms of mesoscale eddies in the NSCS have received much attention in past decades, studies on the reproductivity and predictability of mesoscale eddies in the NSCS are still rare. As mentioned above, mesoscale eddies are not only related to complicated dynamical mechanisms but also involve strong nonlinear processes (Oey et al., 2005). Thus they are not a deterministic response to atmospheric forcing. The quality of mesoscale eddies forecasting will depend primarily on the quality of the initial conditions. Ocean data assimilation, which combines observations with the numerical model, can provide more realistic initial conditions and thus is essential for the
prediction of mesoscale eddies. As shown by previous studies, after assimilating altimeter data into ocean models, the ocean currents in the southern SCS (Xiao et al., 2006) and the realism of three largest eddies in the SCS appear during Typhoon Rammasun (Xie et al., 2018) have been improved. Furthermore, some studies show that the ocean model includes tides or assimilated altimeter data with reasonable MDT, can provide more realistic initial conditions (Xie et al., 2011; Xu et al., 2012). The above studies show that the mesoscale eddies in the SCS are reproducible, but about the predictability of mesoscale eddies is rare. In this study, we assessed the reproduction and predictability of two typical anticyclonic eddies (Wang et al., 2008), owing to be represented different generation mechanisms and survive long enough to be useful, in the NSCS with focus on their generation, evolution and decay processes by a series of numerical experiments based on a Chinese Shelf/Coastal Seas Assimilation System (CSCASS; Li, 2009; Li et al., 2010; Zhu, 2011) along with the observation data from surface drifter trajectory and satellite remote sensing.

2. Datasets and Methodologies

2.1 Datasets

In this study, the altimetric data between 2003-2004, which includes along-track SLA, totally 29 passes (about 9300 points) over the domain of CSCS was selected. Considering the noise of SLA measurement in the shallow seas, data for the shallow areas with depth<400 m was excluded. In order to verify, the merged SLA based on Jason-1, TOPEX/POSEIDON, ERS-2 and ENVISAT (Ducet et al., 2000) provided by
Archiving, Validation and Interpretation of Satellites Oceanographic data (AVISO) at Centre Localization Satellite (CLS, ftp://ftp.aviso.oceanobs.com/global/nrt/) with 1/4° x 1/4° resolution and weekly average are used. In addition, because the SLA present only the anomalies relative to a time-mean sea level field, thus a new mean dynamic topography (nMDT), which has been corrected using iterative method by Xu et al. (2012) was used to calculate the realistic sea level in this study.

In addition to SLA datasets, the daily OISST from the National Oceanic and Atmospheric Administration's (NOAA) National Climatic Data Center (ftp://eclipse.ncdc.noaa.gov/pub/OI-daily-v2/NetCDF/), which was merged by an optimum interpolation method (Reynolds et al., 2007) based on the Infrared SST collected by the Advanced Very High Resolution Radiometer sensors on the NOAA Polar Orbing Environmental Satellite and SST fr Advanced Microwave Scanning Radiometer for the Earth Observing System, are also used. The daily OISST’s biases were fixed using in situ data from ships and buoys. The dataset between 2003 and 2004 was used in this study, with a spatial resolution of 1/4°×1/4°. In addition, the surface drifting buoy data from the World Ocean Circulation Experiment (WOCE, ftp://ftp.aoml.noaa.gov/pub/phod/buoydata/) are also used. A total of 3-Three drifters were designed to drift at the surface within the upper 15 m and tracked by the ARGOS satellite system. Positions of the drifters were smoothed using a Gaussian-filter scale of 24 h to eliminate tidal and inertial currents, and were subsampled at 6 h intervals (Hamilton et al., 1999).

2.2 Method of identify the mesoscale eddies
Similar to the standard of Cheng et al. (2005) and Chelton et al. (2011), we identify
the mesoscale eddies in this study as follows: 1) there must be a closed contour
on the merged SLA; 2) there must be one maximum or minimum inside the area
of the closed contour for anticyclonic or cyclonic eddy; 3) the difference between
the extremum and the outermost closed contour of SLA, that is, the amplitude of the
mesoscale eddy, must be greater than 2 cm; and 4) the spatial scale of the eddy should
be 45-500 km. In addition, the amplitude (A) of an eddy is defined here to be the
magnitude of the difference between the estimated basal height of the eddy boundary
and the extremum value of SSH within the eddy interior: \( A = |h_{\text{ext}} - h_0| \).

2.3 Ocean model

We here used a three-dimensional hybrid coordinate ocean model (HYCOM;
Halliwell et al., 1998; 2000; Bleck, 2002; Halliwell, 2004; Chassignet et al., 2007) to
provide a dynamical interpolator of observation data in the assimilation system.
HYCOM is a primitive equation general ocean circulation model with vertical
coordinates: isopycnic coordinate in the open stratified ocean, the geopotential (or z)
coordinate in the weakly stratified upper ocean, and the terrain following sigma-
coordinate in shallow coastal regions.

In this study, HYCOM was implemented in the Chinese shelf/coastal seas with a
horizontal resolution of 1/12°×1/12°, and in the remaining regions with 1/8°×1/8°, the
model domain is from 0°N to 53°N and from 99°E to 143°E, the detail model domain
and grid can refer to the inset panel of Fig.1. The vertical water column from the sea
surface to the bottom was divided into 22 levels. The K-Profile Parameterization (KPP;
Large et al., 1994), which has proved to be an efficient mixing parameterization in many oceanic circulation models, was used here. The bathymetry data of the model domain were taken from the 2-Minute Grided Global Relief Data (ETOPO2).

To adjust the model dynamics and achieve a perpetually repeating seasonal cycle before applying the interannual atmospheric forcing, the model was initialized with climatological temperature and salinity from the World Ocean Atlas 2001 (WOA01; Boyer et al., 2005) and was driven by the Comprehensive Ocean-Atmosphere Data Set (COADS; Woodruff et al., 1987) in the spin-up stage. After integrating ten model years with climatological forcing, the model was forced by the European Center for Medium-Range Weather Forecasts (ECMWF) 6-hourly reanalysis dataset (Uppala et al., 2005) from 1997 to 2003. The wind velocity (10-m) components were converted to stresses using a stability dependent drag coefficient from Kara et al. (2002). Thermal forcing included air temperature, relative humidity and radiation (shortwave and longwave) fluxes. Precipitation was also used as a surface forcing from Legates and Willmott (1990). Surface latent and sensible heat fluxes were calculated using bulk formulae (Han, 1984). Monthly river runoff was parameterized as a surface precipitation flux in the ECS, the SCS and Luzon Strait (LS) from the river discharge stations of the Global Runoff Data Centre (GRDC) (http://www.bafg.de), and scaled as in Dai et al. (2002).

Temperature, salinity and currents at the open boundaries were provided by an Indian-Pacific domain HYCOM simulation at 1.4°×1.4° spatial resolution (Yan et al., 2007). Surface temperature and salinity were relaxed to climate on a time scale of 100 days. Both two-dimensional barotropic fields such as Sea Surface Height and barotropic
velocities, and three-dimensional baroclinic fields such as currents, temperature, salinity and density were stored daily.

2.4 The assimilation scheme

The ensemble optimal interpolation scheme (EnOI; Oke et al., 2002), which is regarded as a simplified implementation of the Ensemble Kalman Filter (EnKF), aims at alleviating the computational burden of the EnKF by using stationary ensembles to propagate the observed information to the model space. The data assimilation schemes can be briefly written as (Oke et al., 2010):

\[ \hat{\mathbf{\psi}}^a = \hat{\mathbf{\psi}}^b + K (\hat{d} - H\hat{\mathbf{\psi}}^b) \]  
\[ K = P^b H^T [H P^b H^T + R]^{-1} \]

where \( \hat{\mathbf{\psi}} \) is the model state vectors including model temperature, layer thickness and velocity; Superscripts \( a \) and \( b \) denote analysis and background, respectively; \( \hat{d} \) is the measurement vector that consists of SST and SLA observations; \( K \) is the gain matrix; and \( H \) is the measurement operator that transforms the model state to observation space. \( P \) is the background error covariance and \( R \) is the measurement error covariance. In EnOI, Eq. 2 can be expressed as:

\[ K = \alpha (\sigma \circ P^b) H^T [\alpha H (\sigma \circ P^b) H^T + R]^{-1} \]

where \( \alpha \) is a scalar that can tune the magnitude of the analysis increment; \( \sigma \) is a correlation function for localization; and \( P^b \) is the background error covariance which can be estimated by

\[ P^b = AA^T / (n - 1) \]
In Eq. (4), \( n \) is the ensemble size, \( A' \) is the anomaly of the ensemble matrix, \( A = (\psi_1, \psi_2, \cdots, \psi_N) \in \mathbb{R}^{n \times N} \) (\( \psi_i \in \mathbb{R}^N \) (\( i = 1, \cdots, n \)) is the ensemble members, \( N \) is the dimension of the model state, representing usually the model variability at certain scales by using a long-term model run or spin-up run. More detailed description and evaluation of the CSCASS are in Li et al. (2010) and Xu et al. (2012).

3. Results

3.1 The reproduction of these anticyclonic eddies AE1 and AE2 in the NSCS

In order to investigate whether the evolution and migration features of these two eddies can be reproduced by the CSCASS or not, we firstly set up an assimilation experiment named As_exp (see Fig. 4, black line) for AE1 and AE2. In this experiment, the observed SST and SLA are both assimilated into CSCASS at an equal interval of every 3 days. To meet dynamic adjustment, the first assimilation was performed on the 27th of September 2003, two months prior to the generation of AE1.

Based on the As_exp experiment output, we use the observations SLA to evaluate the uncertainty of CSCASS in the research area. In this study, we calculated the weekly mean RMS error (RMSE) of the As_exp/control experiments output and observations for SLA. As the result indicates, the RMSE for the As_exp is between 6 cm to 14 cm, while RMSE for the control is between 10 cm to 18 cm. This result suggested that data assimilation improved effectively the SLA field and had a beneficial impact on model results in this area.

In addition, we also use the Advective Nonlinearity Parameter U/c (ANP, Chelton
et al., 2011; Li et al., 2014; 2015; 2016; Wang et al., 2015) as a criterion to estimate the eddy forecast ability of the CSCASS. As fig. 5 shows, when the ANP is greater than 2 (that is the amplitude greater than 8 cm) AE2 can be well reproduced by the CSCASS. Besides, we also use the independent evaluation, Fig. 6 compared the assimilating results of AE1 with the observations both from the satellite remote sensing and drifter buoys trajectories of number 22517, 22918 and 22610 between December 3rd 2003 and February 18th 2004. From Fig. 6 and Table 1, we can see that the generation and movement of AE1 can be well reproduced by the CSCASS, with the pink curves (assimilation) match well with those of black (satellite observations) and dotted lines (the trajectories of drifter buoys). In addition, the spatial pattern of AE1 can also be well revealed by the CSCASS: the meridional and zonal radii of AE1 detected by the assimilation are 163 km and 93 km, which are almost equal to that of observations (148 km and 79 km). The migration path of AE1 can also be well reproduced by the CSCASS (see Fig. 6, black and pink line) until its amplitude decays to less than 8 cm. In addition to AE1, the generation and evolution of AE2 are also evaluated. As shown in Fig. 7, the evolution and propagation pathway of AE2 (Fig. 7b-7j), e.g. moving northwestward firstly and then southwestward, can generally be reproduced by the CSCASS, although its initial location shows a slight southward bias in the simulation (Fig. 7a). Similar to the results of AE1, discrepancies between model and observations become larger again during the decay phase of AE2. In general, the comparison of assimilation SLA with that of satellite observation and the trajectories of drifter buoys suggested that the generation, development and the
propagation of AE1 and AE2 can be reproduced by the CSCASS when their observed amplitude greater than 8 cm (or the ANP greater than 2). However, when their amplitudes are relatively small, with values less than 8 cm, the features of these two mesoscale eddies are not well reproduced by the CSCASS. This may be related to the value setting of parameter α, the localization length scale, and insufficient spatial resolution of assimilating—assimilated SSH or the numerical model (Counillon and Bertino, 2009).

3.2 The predictability of these anticyclonic eddies in the NSCS

Since the generation, development and the propagation of AE1 and AE2 can be well reproduced by the CSCASS when their amplitude > 8 cm (or the ANP greater than 2), as mentioned above, in this section we further use the CSCASS to investigate the predictability of these two eddies. According to the generation, evolution and migration of these two eddies, we designed six forecast experiments, hereafter referred to as Exp1 to Exp6 (see Fig.4) to investigate their predictability. The model’s initial state prior to each of the six forecast experiments is constrained by assimilating satellite SLA and SST before. Based on the initial state, each experiment is run forward 30 days with the forcing of 6-hourly wind, surface heat flux, and monthly mean river runoff, etc. The first experiment, named Exp1, is applied on the 29th of November 2003, which tends to study whether the generation of AE1 can be forecasted or not. Exp2 is implemented on the 10th of December 2003 and is used to study whether the development and the migration of AE1 can be forecasted. Exp3 is run based on the initial state on the 31st of December 2003 and used to show whether the generation of AE2 and the continued
migration of AE1 can be forecasted. In order to investigate whether the continued
evolution of AE1 and AE2 can be forecasted, Exp4 is applied on the 21th of January 2003. Exp5, is setting up to reveal whether the attenuation of AE1 and the
evolution of AE2 can be forecasted, while Exp6 which is applied on the 29th of February 2004 was designed to find out whether the disappearance of AE1 and AE2 can be forecasted.

The prediction results of Exp1 are shown in Fig. 8. In Fig. 8a, we can see that the forecast is almost coincident with the satellite observation and the trajectory of drift buoys, indicating that the generated position of AE1 can be well forecasted by the CSCASS. In addition, the initial migration of AE1 can also be forecasted by the CSCASS (see Fig. 8a and 8f). In order to evaluate the forecasted amplitude of AE1, the amplitude and the distance of eddy centers between the observation and the forecast are also quantified (Table 2: EXP1). From Table 2: EXP1, we can see that the amplitude of forecasting matches well with that of observation, although its amplitude is slightly larger than that of observation. After 4 weeks, the amplitude of the forecast is still close to those of the observation, suggesting that the generation of AE1 can be well predicted by the CSCASS.

In order to find out whether the development and movement path of AE1 can be predicted after generation, we continue to carry out Exp2. As shown by the observation (Fig. 9), AE1 moves southwestward along the continental shelf with its amplitude decreasing and again increasing after its generation. This observed southwestward movement is also predicted by the CSCASS (see pink closure curve in Fig. 9a-9d),
Although a sudden southwestward movement cannot be well predicted (Fig. 9f). In addition, the first attenuation and then enhancement of AE1 can also be predicted by the CSCASS (see Table 2 and Fig. 9b). On the whole, the development and movement path of AE1 can be well predicted by CSCASS for the first four weeks after its generation. After that, the errors between observation and prediction increase significantly, and by the fifth week, the distance between the center of the prediction and the observation become larger, which more than 100 km (see Fig. 9c).

For further analysis, we carry out Exp3 to look at whether the continued evolution of AE1 and the generation of AE2 can be predicted. This experiment is carried out based on the initial condition of the assimilation on the 31st of December 2003 and the corresponding results are shown in Fig. 10 and Table 2. As shown by the prediction (Fig. 10, Table 2), although with a slightly weak amplitude, the CSCASS can reproduce AE1 after assimilating SLA and SST and predicted its development trend. In addition, the movement path of AE1 cannot be accurately predicted at this period, for instance, the observed AE1 moves directly to southwest (see red solid line and solid circle in Fig. 10f), but the prediction's movement is firstly toward northeast, then turns to southwest (see blue solid line and solid circle in Fig. 10f). The generation of AE2 cannot be predicted in Exp3, which may be related to the smaller amplitude (<8 cm) of AE2 at this period.

The purpose of Exp4 is to look at whether the evolution of AE1 and AE2 can both be reasonably predicted. Since this experiment mainly focuses on the evolution of AE1 and AE2, thus Fig. 11 shows only the evolution of AE2 from the second week after
generation, that is, from the beginning on the 21st of January 2004 to the fifth week. As shown in Fig. 11, Table 2 and Fig. 14d, the trends of amplitude variation of both eddies can be well predicted with the decreasing of AE1 and slowly increasing of AE2. For AE1, the results of the prediction and observation are very close in the first two weeks, with the center of the two almost coincide. The central position of the prediction and observation began to deviate after the third week. For AE2, although the amplitude and movement path are not predicted well at its initial stage, the prediction is slowly approaching to the observation during third to fifth week, and distance between the center of the prediction and the observation is reduced from 132 km at the beginning to 81 km at the end (see Fig. 14d the black solid line).

As mentioned above, the purpose of Exp5 is to investigate whether the decay of AE1 and the continued development of AE2 can be predicted. From Fig. 12, Table 2 and Fig. 14e, we can find that the CSCASS cannot predict the movement path of AE1 well in its decay stage: the distance between the center of the prediction and that of the observation is greater than 188 km, and the movement direction of the two is not consistent (see red lines and dots in Fig. 12f). But the evolution and moving direction of AE2 can be well predicted at this stage. The amplitude of observation and prediction of AE2 are getting closer with timekeeping in the consistent trend (Fig. 14e), although the speed of movement of AE2 given by prediction is slower than that of observation (see blue dashed lines and hollow dots in Fig. 12f).

The aim of Exp6 is to find whether the disappearance of AE1 and AE2 can be both predicted. As described in Fig. 13, the disappearance of AE1 cannot be well predicted
since owing to the low amplitude (less than 8 cm) of AE1 at this stage. Similarly, the
disappearance of AE2 is also less accurately predicted by the CSCASS (Fig. 14f). The
amplitude of AE2 from the observation decays continually at this stage, but the
amplitude of the predicted almost keeps constant. In addition, there is large deviation
of the direction of movement between prediction and observation for AE2 (see the red
solid line and dot in Fig. 13f).

4. Conclusions and challenges for forecasting of mesoscale eddy

In this paper, we carry out a series of assimilation and prediction experiments by
the CSCASS to assess the productivity-production and predictability of mesoscale
eddies in the NSCS, along with observations of satellite observed SST, SLA and the
trajectory data of drift. The comparisons of AE1 and AE2 observations with the
CSCASS prediction experiments, which is assimilated SLA and SST, with that of
observations through predicted experiments shows that when the amplitudes of
mesoscale eddy are higher than 8 cm, the generation, development, decay and
movement of eddies can be well reproduced, but when the amplitude of the mesoscale
eddy is lower than 8 cm, the generation and disappearance of mesoscale eddy cannot
be well reproduced.

The comparisons of AE1 and AE2 through six predicted prediction experiments
with those of observations also show that the generation, evolution and movement path
of these two eddies with high amplitude (>8 cm or the ANP greater than 2) can be well
predicted by the CSCASS, although the generation mechanism of these two
eddies is quite different (Wang et al., 2008). However, when the amplitude of eddies becomes less than 8 cm, the generation position and the movement path cannot be well predicted by the CSCASS.

Our results suggested that for powerful mesoscale eddies, a good initial condition after assimilating observations can help to improve their reproduction and predictability reproduced and predictable ability. As mentioned above, the mesoscale eddies are related to strong nonlinear processes and are not a deterministic response to atmospheric forcing, thus the quality of mesoscale eddies forecast will depend primarily on the quality of the initial conditions. In addition, the ability of the ocean numerical model to faithfully represent the ocean physics and dynamics is also crucial. Although data assimilation, which combines observations with the numerical model, can provide good initial conditions, it cannot make up for the limitations of numerical model in numerical algorithms and in its resolution. Hence, for a high-resolution operational oceanography, the latter means that the numerical models need to be improved using more accurate numerical algorithms and resolution especially in the weakly stratified regions or on the continental shelf.

Furthermore, so far most of the information about the ocean variability is obtained remotely from satellites (SSH and SST), the information about the subsurface variability are very rare. Although a substantial source of subsurface data is provided by the vertical profiles (i.e., expendable bathy thermographs, conductivity temperature depth, and Argo floats), the datasets are still not sufficient to determine the state of the ocean. In addition, in order to accurately assimilate the SSH anomalies from satellite
With the advent of the SWOT (Surface Water and Ocean Topography) satellite mission in 2020, it should be possible to better resolve and forecast the mesoscale features in eddy resolving ocean forecasting systems.

Acknowledgements:

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Fig. 1 Bathymetry of the northern South China Sea. The blue and yellow contour lines are the isolines of 400 m and 1000 m. The solid black Pentagram indicated Dongsha Islands. The migration path of AE1 and AE2 in the NSCS during December 2003–April 2004. Red solid (hollow) circle dots and solid (dash) lines indicated weekly passing position and migration path of observation (assimilation) AE1. Green solid (hollow) circle dots and solid (dash) lines indicated weekly passing position and migration path of observation (assimilation) AE2. The quadrangle and triangle denoted start and end position, respectively. The model domain of CSCSS (the inset panel), the curvilinear orthogonal model grid with 1/8–1/12° horizontal resolution (147×430) is denoted by the blue grid (at intervals of 10 grid cells here).
Fig. 2 Annual mean standard deviation of sea level mesoscale signals (color shading, unit: cm) and propagation velocities of the signals (vectors) derived from (a) altimeter observations; (b) OFES simulations. From Zhuang et al. (2010).

Fig. 3 Snapshots of SLA from satellite remote sensing datasets. Buoy 22918 trajectory (blue lines,
blue asterisk represents the initial position of buoy, as in Fig. 4) (a) from December 4-15, 2003
superposed on SLA field on December 10, 2003; (b) from December 16-23, 2003 superposed on
SLA field on December 17, 2003; SLA field on (c) January 7, 2004; (d) January 21, 2004; (e)

Fig. 4 The settings of assimilation and six forecast experiments, including the start and end date.

Fig. 5 The advective nonlinearity parameter $U/c$ (ANP). The thick red (blue) curve indicates the
ANP of the observed (As_exp experiment) of AE2, the dash line indicates the value of eddy
amplitude at 8 cm or the ANP greater than 2.
Fig. 6 Comparisons of AE1 derived from weekly SLA of assimilation results and observation from satellite remote sensing during the period of December 2003–February 2004. Background color is SLA. "*" mark and closed lines indicated the center position and the outermost closed isoline of AE1, respectively, the black is from satellite observation SLA, the pink is from assimilation SLA. The cyan, green and blue solid circle lines indicated the start positions and trajectories of number 22517, 22918 and 22610 drifter buoys, respectively. (a)-(l) is SLA on the 3rd of December 2003–the 18th of February 2004, respectively. Unit: cm.
Fig. 7 The same as figure 4, but for AE2, the corresponding period is January 28th, 2003–April 14th, 20
Table 1: The amplitude of AE1 and AE2 derived from observation SLA and the assimilation SLA, and distance of eddy centers between the observation SLA’s and assimilation SLA’s.

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Table 2: The amplitude of AE1 and AE2 derived from observation SLA and the six forecast SLA, and distance of eddy centers between the observation SLA’s and forecast SLA’s.

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Fig. 8 Comparison of AE1 of Exp1 and observation, and trajectories of drifter buoys during the 29th of November 2003 and the 29th of December 2004. The cyan, green and blue solid circle dots and lines indicated the start positions and trajectories of number 22917, 22918 and 22610 drift buoys during the corresponding period, respectively. Where, the red (blue) dotted line in (f) is the moving path of AE1 derived from observation (forecast) SLA during the experiment period, the square (triangle) represents the start (end) position.

Fig. 9 Same as figure 8, but for Exp2, the experiment period is the 10th of December 2003 to the 9th of January 2004.
Fig. 10 Same as figure 9, but for Exp3, the experiment period is the 31st of December 2003 to the 30th of January 2004.

Fig. 11 Same as figure 8, but for Exp4, where, the red (blue) dotted line in (f) is the observation (forecast) moving path of AE1 and AE2, the red solid (dashed) lines and solid (hollow) circle derived from observation SLA for AE1 (AE2), the blue solid (dashed) lines and solid (hollow) circle derived from forecast SLA during the 21st of January 2004 to the 20th of February 2004.
Fig. 12 Same as figure 11, but for Exp5, the experiment period is the 8th of February 2004 to the 10th of March 2004.

Fig. 13 Same as figure 11, but for Exp6 and AE2, the experiment period is the 29th of February 2004 to the 30th of March 2004.
Fig. 14 The amplitude of AE1 and AE2 derived from observation SLA and the six forecast SLA, and distance of eddy centers between the observation, assimilation and forecast SLA’s, respectively. The red and green histograms indicated the AE1 amplitudes from observation and prediction respectively. The pink and blue histograms expressed the AE2 amplitudes from observation and prediction respectively. The cyan star solid (dash) line shows the distance of the center between observation and prediction (assimilation) AE1. The black diamond solid (dash) line shows the distance of the center between observation and prediction (assimilation) AE2.