Author’s response to the referee comments on the manuscript of “Atlantic meridional overturning circulation at 14.5° N and 24.5° N during 1989/1992 and 2013/2015: volume, heat and freshwater fluxes”  
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We would like to thank both referees for their comments and suggestions. We found these very important and very helpful for improving the manuscript. Here are the author’s responses to the comments. The referee’s comment is first repeated in black color, followed by the author’s response and the corresponding changes in the manuscript in blue color. After the responses, we include a change-tracking version of the manuscript. The author’s response part has page number in Roman numerals from I to X; the change-tracking manuscript has page number in Arabic numerals from 1 to 65.

Response to the anonymous Referee # 1

I have looked at the work with thoroughness and consider that the authors have made an enormous effort to carry out a series of analyzes and generate significant knowledge about the Atlantic Meridional Overturning Circulation (AMOC). Despite these remarkable efforts, I cannot recommend this article to be published in its current state.

I believe that it is convenient to encourage the authors to review their work and introduce, if they deem it convenient, a series of modifications to make it more robust and ready to be finally published in your journal.

The authors essentially compare volume transports from four zonal hydrographic sections in the North Atlantic, performed with a time difference of 23-24 years, trying to check if in that period the AMOC has intensified or weakened. To do this, they first analyze the distribution of water masses present in the study area and finally use an inverse model to estimate mass transport.

Thank you very much for the thorough examination and the following suggestions.

The main problem I see in the analysis presented is that the authors use for the 1989 section, made at 14.5° N, a reference level different than that used for the other sections. In particular, the reference level chosen is the neutral density ($\gamma_n$) of 27.82 kg/m$^3$, located approximately at 1500 m depth. For the other three sections, they place the reference level at a much greater value ($\gamma_n \approx 28.1295$ kg/m$^3$), located around 4000 m depth. The problem of placing a level of no-motion in the middle of the water column is that the values around that level of no-motion will also be close to zero, reducing notably the mass transports at those levels but allowing the values
located further in depth to increase to unrealistically high values. It can be justified that different reference levels are used for each section, of course, but in this case in which the authors want to compare two sections made at different times, it would have been desirable for the reference level to be the same, so that the differences observed are due to the natural variability in the system and not to an artificiality introduced by the authors.

The inverse model is applied and it could introduce velocities in the reference level, but it actually doesn’t. As it can be seen in the Fig. 8a, the reference level at the stations located in the interior ocean is practically 0. And in Fig. 10a, the no-motion level is clearly located at roughly 1500 m depth. So the initial choice of the reference level is relevant in the remainder of the paper, despite the usage of the inverse model.

If the authors insist on maintaining the current reference levels, it would be convenient for them to carry out some additional analysis in which they show that their results are not altered by the choice of the reference level. In particular, I would like to see what would have happened if the reference level of the section at 14.5° N of 1989 had been made with the deep reference level (γ₀ = 28.1295 kg/m3) or if the section at 14.5° N of 2013 would have been carried out with the shallow reference level (γ₀ = 27.82 kg/m3).

In order to show the impact of the reference level on the inverse solution, we conducted several sensitivity experiments by using different reference levels for the 14.5° N section. The results are summarized in Table R1.

Sensitivity experiments:

- **Experiment 1**, deep reference level (γ₀ = 28.141 kg m⁻³) for the 1989 realization
  
  In this experiment, we use the 1989/1992 box, and shift the reference level of the 1989 realization at 14.5° N from γ₀ = 27.82 to 28.141 kg m⁻³, and keep everything else the same as described in the previous version of the manuscript, except that we have used 0.8 Sv as the Bering Strait transport constraints for both sections.

- **Experiment 2**, shallow reference level (γ₀ = 27.82 kg m⁻³) for the 2013 realization with initial reference velocity
  
  In this experiment, we use the 2013/2015 box, and shift the reference level of the 2013 realization from γ₀ = 28.141 to 27.82 kg m⁻³, then re-calculate the initial reference velocity using this reference level. Other settings are kept the same as described in the previous version of the manuscript.

- **Experiment 3**, shallow reference level (γ₀ = 27.82 kg m⁻³) for the 2013 realization *without* initial reference velocity
  
  In this experiment, except that the initial reference velocity is set to 0, other conditions are kept the same as in Experiment 2.

Results:

- **Experiment 1**
  
  After shifting the reference level of the 1989 realization at 14.5° N from γ₀ = 27.82 to 28.141 kg m⁻³, we see that the thermocline and intermediate layer transports are altered very slightly. Given the same Ekman transport applied in the surface layer, this results in a nearly unchanged AMOC strength. However, the largest
difference occurs in the deep and bottom water layer, especially in the DWBC region. The DWBC transport changes from $-21.5\pm9.6$ (southward) to $6.5\pm9.6$ (northward). The DWBC is defined as the transport between $\gamma = 27.82$ kg m\(^{-3}\), west of 51\(^\circ\) W. Although the total NADW transport does not decrease dramatically, this would mean that the main southward transport in the NADW layers occurs in the eastern half of the basin rather than within the DWBC. Additionally, the AABW transport also strongly decreased from $2.5\pm2.3$ Sv to $-0.3\pm2.3$ Sv. These changes in the deep and bottom water layers are certainly not desirable. This is also the reason that we did not choose $\gamma = 28.141$ kg m\(^{-3}\) as the reference level for the 1989 realization.

**Experiment 2**

Here we use the 2013/2015 box and lifted the reference level of the 14.5\(^\circ\) N section from $\gamma = 28.141$ to $27.82$ kg m\(^{-3}\). In this case, the initial reference velocity is calculated based on the new reference level, and applied. The result indicates that constrained by the initial reference velocity, the inverse solution would change only marginally by shifting the reference level for the 2013 realization at 14.5\(^\circ\) N. The most obvious change is an increase in the DWBC transport by about 4 Sv. This can be expected since a shallower reference level would favor a stronger deep-water transport in the western boundary region, consistent with the results in Experiment 1.

**Experiment 3**

In this experiment, we use the shallow reference level ($\gamma = 27.82$ kg m\(^{-3}\)) for the 14.5\(^\circ\) N section of 2013 but set the reference velocity to zero. In this case, the inverse solution tends to return a weaker UNADW transport ($-3.7\pm2.6$ Sv), but a stronger LNADW transport ($-13.2\pm6.6$ Sv) in comparison to that in Experiment 2. The DWBC transport, as well as the AMOC strength in this experiment is stronger than in Experiment 2.

**Summary:**

For the 1989 realization of the 14.5\(^\circ\) N section, the inverse solution is sensitive to the reference level, and using $\gamma = 27.82$ kg m\(^{-3}\) as the reference level returns more robust features of the AMOC. For the 2013 realization, given the initial reference velocity as a constraint, the inverse solution is insensitive to the reference level, and both shallow and deep level returns consistent solutions. Removing the initial reference velocity would not significantly alter the AMOC strength but would change the structure in the NADW layers. This can be attributed to one of the limitations of the box inverse method. A box inverse model would always minimize the adjustments to the reference velocity to achieve volume conservation, and if a “true” value is too far away from the initial guess, a box inverse model would not be able to retrieve the “true” value without further constraints.

We agree with the Referee that in order to better compare the changes of the AMOC due to its own variability, the reference level for the 14.5\(^\circ\) N section in the two periods should be kept the same. Based on the results of the sensitivity experiments, we decide to use $\gamma = 27.82$ kg m\(^{-3}\) as the reference level for both realizations at 14.5\(^\circ\) N, and constrain the 2013 realization with the initial reference velocity retrieved from the SADCP/LADCP. Additionally, we integrate the sensitivity experiments performed above in section 3.5 of the manuscript.
Comments in detail I would like to make some additional comments:

1. page 1, line 28. The authors’ description of the formation of NADW is perhaps too simple, since not all the heat from the south goes to the formation of NADW but much of it is aimed at heating the climate of Europe. In any case, a reference is needed.

Following this comment, we have changed this sentence to the following:

The warm upper-ocean water carries a large amount of heat from the tropics to the northern latitudes. It loses heat to the atmosphere on its way northward, loses buoyancy, and eventually sinks in the subpolar North Atlantic, returning southward as the cold NADW (Srokosz et al., 2012).

It is now in page 2 line 1-2.

2. page 2, line 22. What type of changes? Changes in the formation rate? Changes in its thermohaline properties?

It is the changes in the transport of LSW. The sentence has been modified as follows:

However, Send et al. (2011) found that at 16° N the interannual variability in the transport of the Labrador Sea Water (LSW; as the primary component of the upper NADW) is responsible for the interannual variability in the AMOC strength.

It is now in page 2, line 26-27.
3. page 3, line 11. Why could it be problematic? Because of the different technology employed?

Because the hydrographic changes over 30 years may have an unknown impact on the inverse solution they obtained.

We therefore have added “due to hydrographic changes over the long period” at the end of the sentence.

It is now in page 4, line 21-22.

4. page 3, line 15. Please, before describing the structure of the paper, its main goal should be more explicitly indicated.

Following this suggestion, we have explained the main goal of this study and enriched the introduction correspondingly.

5. page 5, line 8. The authors describe a treatment performed on the dataset to interpolate and smooth the data for the sections at 14.5°N. Could they provide a sensitivity analysis related to this treatment?

The CTD measurement along the 14.5°N section was operated with an alternating depth between 3000 m and the bottom. To better present the sections at 14.5°N, an interpolation and smoothing method was applied to these data. Please note that this method is used only to smooth and display the sections, neither for the property difference calculation, nor for the transport calculation. In the application of the box inverse model, only the profiles reaching the bottom were used.

A sensitivity analysis of this method is performed by using the salinity and potential temperature sections at 24.5°N. Taking the salinity of the 1992 realization as an example, we first subsample the section by removing the salinity data below 3000 m in every other profile to mimic the case as at 14.5°N. Secondly, we interpolate and smooth the subsampled salinity on to the original grid using the same method as done to the 14.5°N section. Finally, a root mean square (rms) difference is calculated between the interpolated/smoothed salinity section and the original salinity section. The rms for salinity is 0.002 psu. The calculation of the rms for potential temperature is an analogue to the rms for salinity. The rms for potential temperature is 0.018 °C.

6. page 5, line 18. Could the authors also give more transparency to the analysis performed on the oxygen data?

In the western half of the basin at 14.5°N in 1989, we only have bottle oxygen data. In order to present a complete oxygen section, we need to apply a certain interpolation technique. We first tried to interpolate the oxygen data in the vertical and zonal coordinates, but failed due to the very sparse sample position. We then applied a Gaussian weighting function to interpolate the oxygen data in the potential temperature and salinity coordinates. The assumption we made is that oxygen distribution should be related to water mass distribution, because water masses often have their own oxygen characteristics. This Gaussian weighting function is the same as used for interpolating the salinity and temperature data at the 14.5°N section. We first assigned the bottle
oxygen data to the CTD potential temperature and salinity data at the bottle positions, and then interpolated the oxygen data over the full range of all the CTD potential temperature and salinity data in the potential temperature and salinity space. Afterwards, the interpolated oxygen was gridded onto the CTD grid.

To further calibrate the interpolated oxygen, we then calculated a difference between the bottle oxygen and the interpolated oxygen at the bottle positions. Since the bottle positions are scattered, we linearly interpolated the difference onto the CTD grid. Finally, we added this difference to the interpolated oxygen.

7. page 6, line 33. There is a huge dispersion in the observations at those depths. Could the authors show if the differences plotted are significant?

To show that the differences are significant, we calculated the standard error of the mean difference at each depth level, as shown in Fig. R1. The standard error at each depth is calculated as the standard deviation of the difference divided by the square root degrees of freedom (DOF) at each depth level. To calculate the DOF, we divide the total length of the section in the zonal direction by the integral length scale at each depth. The integral length scale is obtained by integrating the area between the first minus and plus zero-crossing of the autocorrelation function of the difference at each depth along longitude.

The results show that the differences in the intermediate-water layer, deep-water layer, and bottom-water layer are significant.

![Figure R1](image)

Figure R1. Zonally averaged (a) salinity and (b) potential temperature differences at 14.5° N. The thick solid lines represent the zonal mean differences, and the thin dashed lines represent the standard error of the mean in both plots.

8. page 7, line 8. At the eastern part of the North Atlantic, the gyre is not so deep to force the variability observed for the water masses at intermediate levels. The authors should consider rewriting this sentence.
This sentence has been rewritten as follows:

On the basin scale, a strengthening of the gyre circulation would bring more AAIW on the western side from lower latitude, while locally, for instance along the eastern margin, higher salinity in the 2015 realization than in the 1992 realization may reflect a seasonal intrusion of the less saline water near the African coast.

It is now in page 10, line 15-17.

9. page 9, line 1. $\Delta x_j$ is presented outside the integral. That would be right if the distance between stations would be regular, which is not the case. The authors should consider writing that element within the integral, as they did in Eq. 12.

10. page 9, line 15. The authors state that they have 51 unknowns. As far as I understood, the inverse model adds 17 unknowns as dianeutral velocities, which are those later shown in Figure 9. The authors should consider rewriting this sentence.

There are 17 unknowns for each property, but we have included dianeutral velocity across each neutral surface for volume, salt anomaly, and heat. As a result, there are 51 unknowns added to the system. Including dianeutral velocity for salt anomaly and heat in a box inverse model has been shown by e.g. McIntosh and Rintoul, 1997 as an effective way of parameterizing the net dianeutral fluxes.

11. page 10, line 5. The authors argue that they must modify meridionally the value of the transport at the Bering Strait (0.8 Sv) that has widely being used to constrain the net transports in zonal sections of the Atlantic Ocean. They state that, otherwise, they would be ignoring the freshwater flux from/to the atmosphere. So, if the freshwater flux between 14.5° N and 24.5° N is a positive value of 0.3 Sv to the atmosphere and the net balance at the zonal section at 24.5° N is 0.8 Sv, then the transport at 14.5° N should be 0.5 Sv. In their argument, the authors are somehow ignoring the freshwater flux in the basin north of the section at 24.5° N, which is unlikely 0.

Not only Hernandez-Guerra et al. (2014) but also Ganachaud (2003) consider that the Bering Strait transport must be used in all the sections of the Atlantic Ocean. The authors should consider reviewing their approach in this point.

We have followed this suggestion and changed the Bering Strait transport to 0.8 Sv for both sections in both boxes, and further removed the surface freshwater flux constraint between the two sections. Since the magnitude of this adjustment is very small, it only changed the inverse results marginally. The text and transport values are modified correspondingly.

12. page 10, line 25. The sentence 'Given the much larger number of unknowns...' could be expanded with '...and
the linear dependency between equations...'

This has been modified accordingly.

13. page 11, line 28. Please, consider producing a picture to explain the method to reference the velocities to those retrieved by the LADCP.

To explain the method of retrieving the reference velocity from the LADCP, we would like to use one of the station pairs as an example. Here we use the station pair located between 25.25° W/14.5° N and 24.50° W/14.5° N, and produce Fig. R2. The red solid curve is the mean LADCP meridional velocity ($V_{LADCP}$) between this station pair; the red dashed line is the barotropic LADCP meridional velocity ($V_{LADCP_{baro}}$), calculated by vertically averaging $V_{LADCP}$ between 200 m and 500 m above the last valid LADCP bin. Using this depth range is to avoid the influence of surface and bottom Ekman layer. The blue solid curve is the relative geostrophic velocity ($V_{geo\_rel}$) between this station pair; the blue dashed line is the mean relative geostrophic velocity ($V_{geo\_rel\_mean}$), calculated by vertically averaging $V_{geo\_rel}$ over the same depth range as done with $V_{LADCP_{baro}}$. The initial guess of the reference geostrophic velocity for this station pair is then the difference between the two dashed lines ($V_{LADCP_{baro}} - V_{geo\_rel\_mean}$). Note that the barotropic tide component should be first removed from the LADCP velocity, which is not shown in this plot.

Figure R2. An example showing the relative geostrophic velocity profile and LADCP meridional velocity profile between the station pair located at 25.25° W and 24.50° W.

14. page 12, line 30. The authors should justify their choice for those uncertainties.

In general, if direct velocity observations are available, the uncertainties of the reference velocity can be estimated based on the observed variability, as we have done for the western boundary of the 14.5 N section in
2013. Since for most part of the sections, the variability of the reference velocity is unknown, the choice of the uncertainties is relatively arbitrary. On the one hand, we have assumed the energetic western boundary currents might have larger uncertainties than the currents in the interior ocean. On the other hand, larger uncertainties in the highly dynamical region means higher weighting in the box inverse model, which would give the reference velocity in western boundary region priority to be solved in the inverse model. We have followed Hernandez-Guerra et al. (2014) to assume an uncertainty at the western boundary of 0.04 cm s\(^{-1}\), and 0.02 cm s\(^{-1}\) in the interior ocean.

We have correspondingly modified the text.

15. page 15, line 20. In Figure 10, the authors present the transports integrated along the layers. A third curve is given, which seems to be the imbalance between the other two curves. However, if we take a close look at the curves, we can see that the imbalance presented is a much smoother curve than the one that should appear after finding the difference between the other two curves. I would ask the authors why the imbalance curve is so smoothed, and why it doesn’t seem to be related to the other two curves. In the left panel of this same figure, please, consider shifting the layer number so it is finally in the layer instead in its interface with the next layer.

The imbalance after the inversion is relatively small and smooth compared to the transport difference in each layer between the two sections because this imbalance is calculated after taking into account the meridional and diazocline transport in and out of each layer from the side and vertical boundaries. To make this point more obvious we now have clarified the imbalance in the caption of Fig. 10 and in the text.

We have now shifted the ticks of the left axis of Fig. 10 and 11 to the middle of each layer.

16. page 16, line 5. The authors consider here that a difference of 1.4 Sv is ‘...very close to each other’, but in the previous page, on line 27, they consider that a difference of 1.6 Sv ‘...is considerably weaker’. They probably should rewrite those sentences.

We noticed this inconsistency and made corresponding modification.

It is now in page 23, line 14-18.

17. page 17, line 12. I would suggest the authors to include a figure showing the velocities in the FC, as they did with the Figure 12.

We have added a Figure 13 showing the meridional geostrophic velocity in the Florida Straits for 1992 and 2015. And correspondingly modify the text describing the Florida Current.

A few typos
1. page 2, line 12: ‘...in detail’
   Changed.
2. page 2, line 23: ‘... were occupied’
We have modified the text in this part, and the original sentence containing this phrase has been deleted.

3. page 3, line 20: '... are given...'
   Changed.

4. page 3, line 24: please, expand here MAR. It’s done later, on page 7, but this is the first time that MAR is used.
   It is expanded.

5. page 5, line 13: '(Figs. 3e-f and 4e-f)'.
   Changed.

6. page 7, line 4: please, expand SAM.
   Done.

7. page 7, line 20: '...originated...'
   Changed.

8. page 15, line 1: 'Note the western...'
   Changed.

9. page 15, line 17: '...only exists...'
   Changed.

X

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Abstract. The Atlantic Meridional Overturning Circulation (AMOC) is analyzed by applying a box inverse model to hydrographic data from trans-Atlantic sections along 14.5° N, occupied in 1989 and 2013, and along 24.5° N, occupied in 1992 and 2015. Direct comparison of water mass properties between the different realizations at the respective latitudes shows that the Antarctic Intermediate Water (AAIW) became warmer and saltier at 14.5° N, and the densest Antarctic Bottom Water became lighter, while the North Atlantic Deep Water freshened at both latitudes. The inverse solution shows that the intermediate layer transport at 14.5° N was also markedly weaker in 2013 than in 1989, indicating that the AAIW property changes at this latitude may be related to changes in the circulation. The inverse solution was validated using the RAPID and MOVE array data, and the GECCO2 ocean state estimate. Comparison between these datasets indicates that the AMOC has not significantly weakened over the past two decades at both latitudes. Sensitivity tests of the inverse solution suggest that the overturning structure and heat transport across the 14.5° N section are sensitive to the Ekman transport, while freshwater transport is sensitive to the transport-weighted salinity at the western boundary.

1. Introduction

The Atlantic Meridional Overturning Circulation (AMOC) plays an important role in the global climate. In the tropical and subtropical North Atlantic, it consists of northward flowing surface, intermediate, and bottom waters, and southward flowing North Atlantic Deep Water (NADW). The warm upper ocean water carries a large amount of heat from the tropics to the northern latitudes. It releases heat to
the atmosphere on its way northward, loses buoyancy, and eventually sinks in the subpolar North Atlantic, returning southward as cold NADW (Srokosz et al., 2012). The net heat transport from the tropics to the higher latitudes has large climate impact (Wunsch, 2005).

Since decades, oceanographers have continuously spent efforts investigating different aspects of the AMOC. For instance, using hydrographic section data obtained during the International Geophysical Year (IGY), and the World Ocean Circulation Experiment (WOCE), many studies focused on estimating the volume transport, and heat and freshwater transports related to the AMOC (e.g., Roemmich and Wunsch, 1985; Macdonald, 1998; Ganachaud and Wunsch, 2000, 2003; Lumpkin and Speer, 2003). These pioneer studies revealed a consistent picture of the AMOC in terms of large-scale horizontal and overturning circulation. Recent studies based on end-point geostrophic mooring data (e.g. Meridional Overturning Variability Experiment, MOVE; and Rapid Climate Change-Meridional Overturning Circulation and Heat Flux Array-Western Boundary Time Series, RAPID-MOCHA-WBTS, hereafter RAPID), have shown that the AMOC exhibits variability on timescales from seasonal to decadal (Cunningham et al., 2007; Kanzow et al., 2008, 2010; Smeed et al., 2014). At 26° N, different components of the AMOC have been analyzed in detail including the western boundary current (Florida Current), the Ekman transport, and the interior geostrophic transport. Based on the RAPID array data, Cunningham et al. (2007) reported that on subseasonal timescales, the upper ocean has an immediate response to the change in the Ekman transport, while Kanzow et al. (2010) showed that on the seasonal timescales, the wind stress curl near the eastern boundary plays a dominant role in modulating the strength of the AMOC. Interestingly, studies based on the RAPID array at 26° N and on the MOVE array at 16° N often reveal contrary conclusions on the AMOC. For instance, RAPID-based estimates indicate that the AMOC decreased at a rate of 4.1±3.2 Sv decade⁻¹ between 2004 and 2013, while MOVE-based estimates indicate a strengthening trend of 8.4±5.6 Sv decade⁻¹ during the same period (Baringer et al., 2015). Smeed et al. (2014) found that a strengthened southward thermocline water transport is responsible for the weakened AMOC at 26° N during 2004-2012, which was balanced by a decrease in the southward flow of the lower NADW. However, Send et al. (2011) found that at 16° N the interannual variability in the transport of the Labrador Sea Water (LSW; as one major component of the upper NADW) is responsible for the interannual variability in the AMOC strength.
Amid the efforts of AMOC observations, changes in water mass properties have also been studied. Curry et al. (2003) compared water mass properties along meridional sections through the Atlantic between 1960s and 1990s, and found that upper-ocean waters generally became warmer and more saline at low latitudes, while at high latitudes waters generally became cooler and fresher throughout the water column. Studies focusing on individual water masses show consistent results, for instance Dickson et al. (2002) show that the source waters of the NADW in the subpolar Atlantic have been freshening since several decades. The freshening signal of the NADW may have crossed the equator reaching the South Atlantic (Hummels et al., 2015). Global Warming and salinification of the AAIW is also observed (Schmidtko and Johnson, 2012). The warming signal of the AABW has been reported crossed the equator reaching the subtropical North Atlantic (Herrford et al., 2017; Johnson et al., 2008).

Continuous changes of properties in a broad range of water masses could be worrying, since recent studies based on model simulations predict a weakening of the AMOC during the 21st century due to accumulated freshening of the northern North Atlantic in a warming climate (Collins et al., 2013; Rahmstorf et al., 2015). Depending on the climate change scenario, the magnitude of the weakening can reach 8 Sv. According to their simulations, the weakening trend of the AMOC should have occurred since decades. A question immediately follows is whether the simulated weakening of the AMOC has been observed. The RAPID AMOC time series to date (April 2004 to Feb 2017) does not show any significant trend, while the MOVE time series (Feb 2000 to Jan 2016) indicate even a strengthening of the DWBC. Note that array-based AMOC observations can only date back to the early 2000s, and they do not provide enough information on water mass property changes. Repeated hydrographic section data provide us opportunity to analyze water mass property changes along the observed sections, and at the same time to examine the circulation if proper methods are applied.

A classical method of estimating the AMOC is the application of a box inverse model to an oceanic box bounded by hydrographic sections and landmasses. By conserving the volume (or mass) and other properties (e.g. heat and salt) in the whole box and layers, the absolute geostrophic velocity (thus the absolute transport) can be obtained (Wunsch, 1977, 1996). In this study, we analyze hydrographic section data along 14.5° N occupied in 1989 and 2013, and along 24.5° N occupied in 1992 and 2015 (Fig. 1). Using these data, we build two boxes in the tropical North Atlantic representing two different

A trans-Atlantic section nominally along 14.5° N was occupied twice in the past, in February-March, 1989, and in May-June, 2013 (Fig. 1). One of the unique features of this section is that it lays roughly at the latitude of maximum annual mean northward meridional Ekman transport (about 8.3 Sv, 1 Sv = 10^6 m^3 s^-1) in the tropical North Atlantic (Fu et al., 2017). Therefore, it is expected that at this latitude, the meridional Ekman transport plays a more important role in the AMOC than at mid-latitudes, for instance, 20° N, especially in terms of meridional heat flux associated with the AMOC.
periods, namely 1989/1992 and 2013/2015. We then apply a box inverse model to each of the boxes and estimate the AMOC for the two latitudes in the different periods.

One of the unique features of the 14.5° N section is that it lays roughly at the latitude of maximum annual mean northward meridional Ekman transport (about 8.3 Sv, 1 Sv = 10^6 m^3 s^-1) in the tropical North Atlantic (Fu et al., 2017). Therefore, it is expected that at this latitude, the meridional Ekman transport plays a more important role in the AMOC than at mid-latitudes, especially in terms of meridional heat transport associated with the AMOC. The 24.5° N section, aligned with the RAPID array, is one of the most frequently surveyed basin-wide zonal sections in the North Atlantic. Many aspects of the AMOC along 24.5° N, in terms of transport components, circulation patterns, and heat and freshwater transports, are well described, and provide reliable information on constraining a box inverse model (Roemmich and Wunsch, 1985; Ganachaud, 2003; Lumpkin and Speer, 2003; Atkinson et al., 2012; Hernández-Guerra et al., 2014). Therefore, we chose this section in combination with the 14.5° N section for the box inverse model, which allow us to pay more attention to the less well studied features associated with the 14.5° N section.

Klein et al. (1995) calculated the meridional transport at 14.5° N from the 1989 realization by applying a box inverse model in combination with the 8° N section occupied in 1957. When compared to modern data (Fu et al., 2017), Klein et al. (1995) used an extremely large annual and seasonal (winter) Ekman transport of 13.58 Sv and 15.94 Sv for the calculation, in contrast to an annual mean of 8.29±2.59 Sv calculated from the National Centers for Environmental Prediction Climate Forecast System Reanalysis (NCEP/CFSR) monthly wind stress data. Besides, the large time difference between the occupations of the two sections (more than 30 years) could be problematic in the application of a box inverse model due to hydrographic changes over the long period. As a result, the derived transports of northward flowing water masses (e.g. Antarctic Intermediate Water, AAIW and Antartic Bottom Water, AABW) were surprisingly small. Therefore, it is also necessary to revisit the 1989 realization of 14.5° N in order to obtain a more reliable meridional overturning circulation for that year.

Provided with the hydrographic sections and box inverse method, we first identify changes of water mass properties along the two sections between 1989/1992 and 2013/2015, and then determine whether the AMOC in the tropical Atlantic has significantly changed over the past two decades. Note that both
the 2013 and 2015 realizations are so far the newest available data at the corresponding latitudes, which would help to update our knowledge of water mass properties and the AMOC at these locations. The paper is organized as follows: In section 2, the data used in this study are introduced, and the water mass distribution and the property changes between the two periods along the two latitudes are described. The details of the box inverse model and the calculation methods for the heat and freshwater transports are given in section 3. The inverse model results are presented and discussed in section 4. A comparison between the inverse solutions, GECCO2 ocean state estimate, and the MOVE and RAPID array analysis data is presented in section 5. Conclusions are given in the final section.

2 Hydrographic data and water masses

2.1 Hydrographic sections at 14.5° N and 24.5° N

The first survey of the 14.5° N section was from 5 to 23 February 1989, and jointly completed by R/V Meteor (M09) and R/V Albatross IV, covering the eastern and western half of the section separated by the Mid-Atlantic Ridge (MAR, at about 42.5° W), respectively. At the western boundary, the cruise track of R/V Albatross was northeastward from 11.3° N/60.3° W to 14.5° N/ 57.5° W. It was necessary in order to complete the section perpendicular to the continental slope and to sample the western boundary currents (including the deep western boundary current, DWBC) there. During the cruise, Conductivity-Temperature-Depth (CTD) measurements were conducted. At the western boundary, all of the CTD profiles (westernmost 10 profiles) reached the bottom with an averaged horizontal spacing of 30 nm, for the rest of the section, the CTD depth alternated between the bottom and 2000 m with an averaged horizontal spacing of 45 nm. As a result, 39 CTD profiles in total reached the bottom for the entire section with a 1-m vertical resolution. The accuracy of the data set is expected to be ±0.002 °C for temperature, ±0.002 psu for salinity, and ±3 dbar for pressure, respectively (Klein et al., 1995). The M09 CTD was also equipped with a Beckmann type polarographic oxygen sensor that measured the oxygen current (OC/A) and oxygen temperature (OT/°C). They were converted to dissolved oxygen concentration according to Owens and Millard (1985) and calibrated using the available bottle oxygen data. The final processed CTD oxygen data have an accuracy of ±10 µmol kg⁻¹ (using a double root
mean squared difference against bottle oxygen data). The R/V Albatross CTD oxygen sensor malfunctioned; only bottle oxygen data were available. The processing details of the R/V Albatross and R/V Meteor CTD data have been described in Wilburn et al. (1990) and Klein (1992).

The second survey of the 14.5° N section was done in 2013 aboard R/V Meteor during the cruise M96 (28 April to 20 May 2013) and M97 (8 and 9 June 2013). The M96 leg covered the section from the coast of Trinidad and Tobago (11.3° N/60.3° W) to about 20° W, and during the M97 leg the measurements were continued from 20° W to the African coast (easternmost 4 stations). During the cruises, CTD measurements were performed on a grid similar to that of 1989. The westernmost part of the section (10 stations) was perpendicular to the coast and all profiles reached the bottom; for the rest of the section, CTD depth alternated between the bottom and 3000 m. In total 64 CTD stations were occupied along the 14.5° N section with a nominal resolution of 40 nm, and 48 profiles reached the bottom with a 1-m vertical resolution. The CTD work was carried out using a Sea-Bird Electronic (SBE) 9 plus system with double sensor packages for temperature, conductivity and oxygen. The accuracy of the temperature sensors is ±0.001 °C; after calibration by comparing the bottle stop salinity and oxygen with the measurements of salinometer and oxygen titration of bottle samples, the accuracy of salinity and oxygen sensors is ±0.002 psu and ±1.3 µmol kg⁻¹, respectively. Different from the 1989 occupation, the 2013 occupation also included direct velocity observations. During the M96 leg, two 300 kHz Teledyne RDI Lowered-Acoustic-Doppler-Current-Profilers (LADCP) were mounted to the CTD-Rosette for most of the stations, except for stations between 38° W and 33.5° W, where the large water depth (>6000 m) prevented the use of the LADCPs. During the M97 leg, no LADCP system was installed. The LADCP data was post-processed with the GEOMAR processing routine v10.4 (Fischer and Visbeck, 1993; Visbeck, 2002). Additionally, two shipboard Teledyne RDI ADCP (SADCP) were in operation at frequency of 38 kHz and 75 kHz. They are equipped with phased array transducers and can measure up to 1200 m and 800 m depth, respectively. Ship navigation information was synchronized with the system. Misalignment angles and amplitude factors were calibrated during the post processing. The uncertainties of 1-hour averages of the underway measurement is expected to be 2-4 cm s⁻¹ (Fischer et al., 2003).
At 24.5° N, the CTD section has been repeated several times (Atkinson et al., 2012). In this study, we chose data measured during cruises from 14 July to 15 August 1992, and from 10 Dec 2015 to 20 Jan 2016 to combine with the 14.5° N section measured in 1989 and 2013, respectively. The CTD data were provided through the CLIVAR and Carbon Hydrographic Data Office (CCHDO). All the profiles reached tens of meters above the ocean bottom with a 2-m vertical resolution. The distance between the adjacent CTD stations was typically 25 to 30 nm. When surveying across boundary currents and continental slopes, the distance was reduced to resolve the boundary current structure. Within the Florida Straits, 11 profiles were collected as part of the 1992 section. During the 2015 occupation, Florida Straits was surveyed twice, but only profiles collected during the first survey were used in this study due to the higher spatial sampling resolution.

2.2 Water mass distribution and property changes

The water mass properties at 14.5° N have been introduced by Molinari et al. (1992) and Klein et al. (1995) based on the 1989 realization. At 24.5° N, the water mass properties have been described extensively (e.g. Roemmich and Wunsch, 1985; Hernández-Guerra et al., 2014). Here we briefly describe the water mass properties and emphasize property differences between 1989/1992 and 2013/2015 along the two sections. The potential temperature (\(\theta\)) and salinity (\(S\)) diagram drawn using data at the two sections provides an overview of the distribution of water masses (Fig. 2). The vertical sections of salinity, potential temperature, oxygen (\(O\)), and neutral density (\(\rho_n\)) are presented for the different years at each section in Fig. 3-6.

As described in the previous section, at 14.5° N, except in the western boundary region, the CTD depth alternates between 2000 m (3000 m) and the ocean bottom for the measurement in 1989 (2013). For a better visual effect, a Gaussian weighting function with horizontal influence and cut-off radii of 0.5 and 1.5 degree in longitude, vertical influence and cut-off radii of 20 and 40 m were applied to interpolate and smooth the data. The horizontal and vertical resolution of the mapping was chosen as 0.25 degree and 20 m. At 24.5° N, no interpolation and smoothing are needed due to the high horizontal resolution. The difference of \(S\) and \(\theta\) between the two time periods for each section is also shown to facilitate the discussion (Fig. 3e-f and 4e-f). To calculate the difference, the original \(S\) and \(\theta\) were firstly transformed.
from pressure levels to uniform $\gamma_n$ levels, then they were horizontally interpolated on each $\gamma_n$ level onto a consistent horizontal grid; finally, the differences of $S$ and $\theta$ were calculated between the two time periods, and transformed back to pressure level and smoothed using a Gaussian weighting function as described above.

At 14.5° N, only bottle oxygen data are available in the western half of the basin for the 1989 dataset (the Albatross IV leg). To obtain an oxygen section on the same regular grid, the bottle oxygen, $\theta$ and $S$ data were used to derive oxygen as a function of $\theta$ and $S$ in the $\theta/S$ space. Here a Gaussian interpolation function was applied to achieve a general functional relationship that finally allowed obtaining an oxygen distribution from the $\theta$ and $S$ distribution along the section. To further correct for local variations that may not have been correctly represented by the functional relationship, we calculated an oxygen anomaly as the difference between derived oxygen and bottle oxygen data. The oxygen anomaly was interpolated onto the grid of the section and finally subtracted from the derived oxygen field. In this way, both general and local relations of the oxygen to the water masses were taken into account. The remaining eastern part of the 1989 oxygen section is directly from the CTD Beckman type oxygen sensor (cf. Section 2.1).

The water mass distribution can be inferred from the $\theta$-$S$ diagram (Fig. 2). At 14.5° N, proceeding from the surface, the long tail with homogeneous temperatures above 25 °C represents the surface water mainly in the mixed layer. The different temperature levels (with a mean offset of 1.60 °C in the upper 50 m) are most likely caused by the different seasons when the occupations took place (February 1989 and May 2013, respectively). Slightly below the surface water, a salinity maximum at about 24 °C marks the Subtropical Underwater (STUW), corresponding to the subsurface layer centered at about 120 m in Fig. 3a and 3c. This water mass originates from the subtropical Atlantic, where evaporation exceeds precipitation, forming sea surface salinity (SSS) maxima at about 25° N in the North Atlantic (as shown in Fig. 3b and 3d at 24.5° N) and about 20° S in the South Atlantic. The salinity maximum waters are further subducted and transported equatorward and westward as part of the subtropical cells (McCreary and Lu, 1994; Schott et al., 2004). The median $\theta$-$S$ diagram calculated on neutral density surfaces at 14.5° N shows two salinity maxima between 22 and 25 °C (Fig. 2a), indicating the presence of northern and southern origin of these water masses (Klein et al. 1995).
Within the temperature range from 20 to 8 °C, the majority of water has a nearly linear $\theta$-$S$ relationship for both sections (Fig. 2) that is a characteristic of Central Water (CW). CWs compose the main thermocline and are formed by subduction in the subtropical gyre. As a result of subtropical gyre circulation, CWs occupy a larger depth range in the west than in the east, which can be seen from the upward tilting of the isotherms toward east (Fig. 4a to 4d). Within the temperature range between 13 and 18 °C, a deviation from the linear $\theta$-$S$ relation is found at the 14.5° N section from profiles sampled east of 22° W, where the Cape Verde Frontal Zone (CVFZ) is located. East of the CVFZ, signatures from South Atlantic Central Water (SACW) are seen, which is less saline than North Atlantic Central Water (NACW). The SACW takes routes along and parallel to the equator following, after crossing the equator in the western equatorial Atlantic, the different eastward jets of the tropical North Atlantic. When approaching the West African coast, it spreads further northward from where it diffuses into the eastern tropical North Atlantic (Kirchner et al., 2009; Brandt et al., 2015). The CW layer at 24.5° N consists primarily of NACW.

At 14.5° N, the CW layer is characterized by low dissolved oxygen (DO) concentration down to 40 $\mu$mol kg$^{-1}$ at its core (Fig. 5a, c). This layer is within the Oxygen Minimum Zone (OMZ) in the eastern tropical North Atlantic, which is formed generally due to weak ventilation and oxygen consumption (Luyten et al., 1983; Brandt et al., 2015). Comparing the OMZ between 2013 and 1989, it shows that the thickness of the minimum oxygen core (DO<60 $\mu$mol kg$^{-1}$) increased, while the westward extent of this core reduced. Such changes created a complicated pattern of the DO difference between 2013 and 1989 (not shown). First of all, the vertical expansion of the minimum oxygen levels are in agreement with the findings by Stramma et al. (2010), and is associated with a local decrease of DO below the near-surface layer down to 500 m along the eastern boundary (west of 22° W). On the other hand, the reduction of its zonal extent led to an increase of DO to the east of the core position in 2013, indicating that the oxygen decrease is not spatially coherent with local processes, and/or that processes on shorter timescales might affect the oxygen evolution.

Directly below the CW is the intermediate water layer. At 14.5° N this layer consists predominantly of AAIW, while at 24.5° N AAIW and Mediterranean Water (MW) are both main contributors to this layer. AAIW is characterized by its salinity minimum centered at around 900 m (Fig. 3a and 3c), while
MW is warmer and saltier. The AAIW in the North Atlantic originates from the South Atlantic just north of the Antarctic Circumpolar Current, and is transported northward mainly along the western boundary (Tsuchiya, 1989). As a consequence of mixing with the surrounding waters on the way toward the north, AAIW gradually loses its salinity minimum signature in the northern hemisphere from the tropics to the subtropics. This can also be seen when comparing the 14.5° N and 24.5° N sections.

From the θ-S diagram (Fig. 2a, c) and the vertical sections (Fig. 3e and 4e), it can be seen that the AAIW at 14.5° N became saltier and warmer between 1989 and 2013. This result is consistent with the previous studies on AAIW by Sarafanov et al. (2008), who found a significant warming of the AAIW at 6.5° N between 1993 and 2000. Schmidtko and Johnson (2012) reported a warming and salinification trend in the AAIW core since 1970s throughout the tropical North Atlantic. They have attributed the warming trend to higher sea surface temperature in the AAIW formation region in the background of global warming, and to a strengthened Agulhas leakage associated with a low Southern Annular Mode (SAM) during some periods of the 20th century. At 24.5° N, between 2015 and 1992, the waters in the intermediate layer became generally cooler and fresher in the western half of the section, while warmer and saltier in the eastern half of the section (Fig. 3f and 4f). Since the intermediate water at 24.5° N is composed of both AAIW and MW, the property change over time could be considered as an imprint of changing relative contributions of AAIW and MW along the section. On the basin scale, a strengthening of the gyre scale circulation would bring more AAIW on the western side from lower latitude, while locally, for instance along the eastern margin, higher salinity in the 2015 realization than in the 1992 realization may reflect a seasonal intrusion of the less saline water near the African coast (Roemmich and Wunsch, 1985; Hernández-Guerra et al., 2005). MW has been reported to occupy a greater portion of the eastern boundary during late winter and early spring, while AAIW contributes more in late fall and early winter (Hernández-Guerra et al., 2003; Fraile-Nuez et al., 2010). Machín et al. (2009, 2010) explained the seasonally varying contribution of the AAIW and MW with the stretching and shrinking of the intermediate water strata. Mediterranean eddies appeared at 24.5° N in both realizations and caused the maximum salinity values at about 7 °C in the θ-S diagram (Fig. 2b).

The NADW originates from the subpolar North Atlantic and is found at both sections (14.5° N and 24.5° N) in the γγγ range of 27.922–28.141 kg m⁻³. According to its formation region and the
corresponding density ranges, NADW can be divided into Upper NADW (UNADW), which is composed primarily of water formed in the Labrador Sea (LSW) (Talley and McCartney, 1982), and Lower NADW (LNADW), originated from water masses formed in the Nordic Seas (Pickart, 1992; Smethie et al., 2000), namely Iceland-Scotland Overflow Water (ISOW) and Denmark Strait Overflow Water (DSOW). At both sections, a sharp isoneutral (surface of the same neutral density) slope in the NADW layers at the western boundary is indicative of the DWBC and its recirculation. The DWBC seems to be a continuous feature between 24.5° N and 14.5° N, which is evident from the elevated oxygen concentration (DO>260 µmol kg⁻¹) along the continental slope at the western boundary (Fig. 5) due to a more recent contact with the atmosphere compared with surrounding waters in a similar density range. A dual-core structure of high oxygen at the western boundary is captured at 14.5° N in 2013, resulting from the ISOW with relatively low oxygen laying between the oxygen-rich LSW and DSOW. At 24.5° N, even higher oxygen concentration (DO>270 µmol kg⁻¹) is found in the DWBC region centered at about 3300 m in 2015, indicating the presence of more recently ventilated contributions to the LNADW. Throughout the NADW layers, the water became fresher and cooler on neutral density surfaces at both sections. The freshening is in agreement with previous studies showing that the NADWs in the formation region has been freshening since decades (Dickson et al., 2002), and that the freshening signal has also been observed near the western boundary in the South Atlantic at 5° S and 11° S (Hummels et al., 2015).

Isotherm and isohaline surfaces do not continue from the western into the eastern Atlantic across the MAR, lower temperature and salinity but higher density is found in the western basin (west of the MAR) due to the influence of less saline and colder but also denser AABW (e.g. Klein et al., 1995). AABW is the densest water in the world oceans and is present at both 14.5° N and 24.5° N primarily in the western basin with γ₀ larger than 28.1250 kg m⁻³ and θ lower than 1.80 °C. The MAR, as a topographic barrier, prevents AABW flowing directly into the eastern Atlantic basin, except at the Romanche Fracture Zone near the Equator and the Vema Fracture Zone at 11° N (Wüst, 1935; McCartney et al., 1991). Klein et al. (1995) reported that the lowest salinity and temperature in the eastern basin found at 14.5° N was lower than that found at either 16° N and 8° N, indicating that a pathway for AABW crossing the MAR existed between 8° N and 14.5° N. It is believed that AABW
gets warmer and saltier on its way to the north due to mixing with the overlying LNADW, therefore, it is not surprising that the densest AABW is warmer and saltier at 24.5° N than at 14.5° N. It appears that at both latitudes, the AABW became cooler and fresher between the two periods (Fig. 3e, f and 4e, f). Note that we have calculated the changes on neutral surfaces, if the difference is calculated on pressure surfaces, it presents a different and complex picture (not shown). For example, at 14.5° N, the pressure-based difference shows that the AABW became warmer and saltier west of 55° W, while cooler and fresher east of 55° W. At 24.5° N, the pressure-based difference shows that the AABW became mostly warmer but fresher, which is consistent with the previously observed warming of AABW at 24.5° N by Johnson et al. (2008), who also calculated the changes on pressure surfaces. At the same time, we noticed that the density of densest AABW observed at 14.5° N reduced from 28.1686 kg m⁻³ in 1989 to 28.1623 kg m⁻³ in 2013, and at 24.5° N from 28.1596 kg m⁻³ in 1992 to 28.154 kg m⁻³ in 2015. As a result, we believe that the warming of the AABW at 14.5° N and 24.5° N should not arise from property changes on the density surface, but should be due to depletion of the densest AABW core ($\gamma_a > 28.141$ kg m⁻³) at both latitudes. This agrees with Herrford et al. (2017), who showed that in the equatorial South Atlantic, the coldest AABW became warmer since the early 1990s.

3 Methods

3.1 Inverse model setup

The box inverse method was applied to determine the meridional overturning transport across the 14.5° N and 24.5° N sections. Two “boxes” bounded by the ocean boundaries and the hydrographic sections measured in 1989/1992 (1989/1992 box) and 2013/2015 (2013/2015 box), respectively, can be built. Based on the thermal wind relation, the vertical shear of the geostrophic velocity relative to an arbitrary reference depth can be calculated from the density field between adjacent CTD stations. To obtain the absolute geostrophic velocity, a reference velocity must be assigned to the shear at the reference level. A box inverse model is composed of equations that employ the thermal wind relation and conservation of properties (i.e. volume, salt, heat, Eq. 1). It adjusts the reference geostrophic velocity and vertical
fluxes of properties from prior (initial) estimates to conserve the properties within the whole box and each layer of the box.

Following Ganachaud (2003) and Hernández-Guerra et al. (2014), we separated the two boxes into 17 vertical layers by neutral density surfaces specified according to the characteristics of water masses (Table 1). In this study, we applied the conservation of volume, salt anomaly, and heat at each layer and the whole box. The salt anomaly was calculated by subtracting a section-areal mean salinity from the salinity values. The conservation equation of a property \( C \) in a layer can be formulated in the general form

\[
\sum_{j=1}^{J} \int_{h_{m}}^{h_{m+1}} \left( v_j + b_j \right) C_j \Delta x_j \, dz \, + \, \left[ -w^C_m A_m C_m + w^C_{m+1} A_{m+1} C_{m+1} \right] \approx 0 ,
\]

where \( j \) and \( m \) are indices for station pairs and layer interfaces, respectively; \( J \) is the total number of station pairs; \( \Delta x_j \) represents the horizontal distance between station pair \( j \); \( h_m \) refers to the depth of layer interface \( m \); \( v_j \) and \( b_j \) are the relative and reference geostrophic velocities at station pair \( j \), respectively; \( C_j \) and \( C_m \) are the property concentration at station pair \( j \) and interface \( m \), respectively; \( w^C \) is the dianeutral velocity of property \( C \) at the layer interfaces; \( A \) refers to the horizontal area of the layer interfaces within the boxes. Eq. 1 states that the total change of property \( C \) in one layer due to horizontal advections through the side boundaries and vertical fluxes through the upper and lower boundaries is approximately 0. Note that we defined a dianeutral velocity for each property including the volume, salt anomaly, and heat. This has been proven to be an effective way of parameterizing the net dianeutral fluxes in inverse models (McIntosh and Rintoul, 1997; Sloyan and Rintoul, 2001; Tsubouchi et al., 2012).

Except \( b \) and \( w \), all other quantities in Eq. 1 are either known, or can be directly estimated from the hydrographic and topographic data. Note that for both realizations at 14.5° N, only profiles approaching to the bottom were used to construct the box inverse model (see Sect. 2.1 for details). For the 1989/1992 box, there are 149 CTD station pairs, the adjustment to the reference velocity at each station pair is treated as an unknown; the dianeutral velocity for each property across each layer interface is treated as an unknown, which adds 51 unknowns to the system. For the 2013/2015 box, there are 228 unknowns.
in total, including the adjustment to the reference velocity of 177 CTD station pairs and 51 dianeutral velocities.

3.2 Constraints

To seek solutions for the unknowns \( b \) and \( w \), other transport constraints at specific locations and depths can be applied in addition to the conservation equations of the properties in each layer and the whole box (Eq. 1). The details of the additional constraints are described here and summarized in Table 2. At 24.5° N, following Hernández-Guerra et al. (2014), we assumed a DWBC transport of \(-26.5\pm13.5 \text{ Sv} \) (“-” denotes southward). The uncertainty range was given by half of the DWBC transport, when the large uncertainty in the different estimates based on moored observations was taken into account (Bryden et al., 2005; Johns et al., 2008; Meinen et al., 2013). This value was then applied to both time periods as the a priori constraint of the DWBC at 24.5° N between layer 7 and 14, 77° W and 72° W.

A continuous time series of the Florida Current (FC) transport has been constructed by using a succession of the submerged telephone cables across the Florida Straits between 26° N and 27° N (Baringer and Larsen, 2001; Meinen et al., 2010). In this study, the FC transport was constrained using the annual mean value of 31.3±1.1 Sv in 1992 and 31.7±1.1 in 2015, calculated from the daily FC transport data. The uncertainties were given by the standard deviation of the annual mean FC transport between 1982 and 2016 estimated using the daily data. Note that both values are not significantly different from a long-term mean FC transport of 31.1±2.4 Sv (adopted from Atkinson et al., 2010).

Using the long-term mean value as the constraint for both boxes would only alter the final solutions marginally.

About 0.8±0.6 Sv water flows from the Pacific to the Atlantic through the Bering Strait (Roach et al., 1995; Woodgate et al., 2005). Following Ganachaud (2003) and Hernández-Guerra et al. (2014), we constrained the Bering Strait transport through both sections as 0.8±0.6 Sv in both boxes.

At 14.5° N, an additional constraint on the AAIW transport of 2.8±2.1 Sv for the 2013 realization was applied. We found that without this additional constraint, the final AAIW transport for the 2013 realization after the inversion would be southward, regardless what reference level or whether an a priori reference velocity based on the ADCP measurement was applied. This is contrary to the expected...
AAIW flow direction. Therefore, we constrained this quantity based on the annual mean AAIW transport from the monthly data of the dynamically consistent and data-constrained ocean state estimate GECCO2 (Wunsch and Heimbach, 2006; Köhl, 2015) at 14.5° N in 2013. The uncertainty is given by the standard deviation of the monthly AAIW transport in GECCO2 at 14.5° N between 1985 and 2015. The AAIW in GECCO2 is defined using the same neutral density range (27.38<\gamma<27.82 \text{ kg m}^{-3}) as for the observed hydrographic data.

The Ekman transport in the box inverse model is prescribed in the first layer of each section, which was estimated using the monthly wind stress data from the NCEP/CFSR (from 1949 to 2010) and NCEP/CFS Version 2 (NCEP/CFSv2, from 2011-present). The annual mean Ekman transport in the calendar year of the cruise was used (cf. Table 2 for the values).

Considering the above listed additional constrains and the conservation equations for the properties in each of the 17 layers and the whole box, we can formulate in total 59 equations for the 1989/1992 box, and 60 equations for the 2013/2015 box. Given the much larger number of unknowns and the linear dependency between equations, the box inverse model is always an underdetermined system. Conventionally, the equations can be written in a matrix form

$$ Ax = b, $$

where $A$ is a $M \times N$ matrix that consists of areas of the station pairs in layers multiplied by the property concentration, and areas of the neutral density surfaces multiplied by the property concentration on that surface; $x$ is a $N \times 1$ matrix of unknowns that consist of reference geostrophic velocity at the station pairs and dianeutral velocity for the properties; $b$ is a $M \times 1$ matrix that consists of property transport due to the relative geostrophic velocity; $M$ is the number of equations; $N$ is the number of unknowns.

3.3 Reference level and a prior reference velocity

The reference level for the geostrophic velocity calculation must be chosen first. An ideal choice would be a level of no motion, but which is rarely found in the real ocean. Therefore, a density surface that separates the northward flowing water masses (i.e. AAIW and AABW) from the southward flowing water masses (i.e. NADW) is preferable for the reference level with zero velocity as an initial guess (Klein et al., 1995; Ganachaud et al., 2000). For the 14.5° N section, the reference level for both
realizations was chosen following Klein et al. (1995) as the surface of $\gamma_s = 27.02 \text{ kg m}^{-3}$, which separates the AAIW and the UNADW. For the two realizations along the 24.5° N section, the reference level was defined by $\gamma_s = 28.141 \text{ kg m}^{-3}$, which separates the LNADW and AABW (Ganachaud et al., 2000; Hernández-Guerra et al., 2014). The neutral surfaces with $\gamma_s \geq 28.141 \text{ kg m}^{-3}$ tilt upward toward the east on the western side of the MAR. Therefore, it would favor a northward flow in the AABW layers when using $\gamma_s = 28.141 \text{ kg m}^{-3}$ as the reference level with zero reference velocity (Fig. 6). For all the sections, when the corresponding density level is deeper than the deepest common depth of the adjacent CTD station pairs, the deepest common depth was then chosen as the reference level. The bottom triangle was set by constantly extrapolating the velocity at the deepest common depth to the bottom. Using these reference levels with zero reference velocity for the sections results in an AMOC-like meridional transport with, for instance, water in the NADW layers (layer 7 to 14) generally flowing southward, and in the bottom layers (layer 15 to 17) flowing northward. However, the imbalance between the two sections has the same order of magnitude as the initial transport itself, indicating that the volume is not conserved in individual layers and the whole box at this stage. Here “initial transport” corresponds to the transport derived from the geostrophic velocity assuming zero velocity at the chosen reference levels.

In the lack of a prior knowledge on the absolute velocity field, the reference velocities at the reference level are assumed to be 0. This is the case for both realizations at 24.5° N, and for the 1989 realization at 14.5° N. During the occupation along 14.5° N in 2013, both SADCP and LADCP were operated. These direct velocity observations provide valuable information about the velocity at the reference level. Dengler et al. (2002) showed that the vertically averaged LADCP velocity could serve as the reference geostrophic velocity for the corresponding CTD station pairs with an accuracy of 0.012 m s$^{-1}$. Following their method, the barotropic tide component was first removed from the cross-section LADCP velocity, and then the tide-removed LADCP velocity was averaged between the adjacent CTD stations. The barotropic tide velocity was estimated by using the Tide Model Driver (TMD) (Egbert and Erofeeva, 2002). Fu et al. (2017) showed that for the 2013 realization, meridional ageostrophic velocity existed mainly in the upper 200 m. Hence, the cross-section LADCP velocity and relative geostrophic velocity were averaged vertically between 200 m and 50 m above the bottom to avoid the influence of...
any ageostrophic component. Finally, the difference between the vertically averaged LADCP and
relative geostrophic velocity was calculated to represent the reference geostrophic velocity. Note that at
the western boundary region (westernmost 6 station pairs west of 57.5° W), cross-section velocity from
the 38-kHz SADCP was used instead of LADCP velocity. Because the water depth is relatively shallow
(less than 1300 m), and the 38-kHz SADCP covered most of the water column with a much higher
horizontal resolution (10-minute ensembles), which makes the horizontal average of the SADCP
velocity profiles between the CTD stations more preferable than the two-profile average of LADCP
velocities. As shown in Fig. 7, the reference velocity for the 2013 realization at 14.5° N shows large
positive values at the western boundary, indicating a boundary intensified current. The error bars for
station pairs 1-6 were estimated from the root mean squared error of the vertically averaged SADCP
velocity (in the range of 200 m and 50 m above the last reliable bin) between each station pairs; for the
rest of the station pairs, the uncertainties were given as 0.04 m s⁻¹ in the western basin and 0.02 m s⁻¹ in
the eastern basin, which are larger than the value estimated by Dengler et al. (2002), but is generally
assumed for the reference velocity in box inverse model studies (e.g. Ganachaud, 2003).

3.4 Weighting and error estimates

The solution of the box inverse model depends on the a priori knowledge about transport variation as
well as uncertainties in the reference velocity field. This can be translated into a row weighting matrix
\( W \) (\( M \times M \)) and a column weighting matrix \( E \) (\( N \times N \)), which were applied to the system before
inversion. Following Tsubouchi et al. (2012), the row weighting for volume conservation is defined as

\[
W_{\text{v}} = \frac{1}{\varepsilon_m},
\]

where \( \varepsilon_m \) is the a priori volume transport uncertainty for each layer and additional constraints (e.g. FC
transport, DWBC, etc.). For property conservation, the row weighting is defined as

\[
W_{\text{p}} = \frac{1}{\sigma \eta_m}
\]

where \( \sigma_m \) is the standard deviation of properties within layer \( m \). To take into account a possible
correlations between the section averaged and mesoscale components of the noise in the property
conservation equations, a factor of 2 was introduced in the denominator in the right hand side of Eq. 4
(Ganachaud and Wunsch, 2000; Tsubouchi et al., 2012). Following Ganachaud (2003), we set the uncertainties for volume conservation equations to gradually decrease from 8.2 Sv in the surface layer to 0.5 Sv in the bottom layer, and 15.9 Sv for the whole box.

The column weighting was set based on the a priori uncertainties of the reference velocity, $\delta b_j$, and the diurnal velocity, $\delta w_m$. For the reference geostrophic velocity, the column weighting is

$$E_j = \left(\frac{\delta b_j}{A_j}\right)^{1/2},$$

and for the diurnal velocity, the column weighting is

$$E_m = \left(\frac{\delta w_m}{Q_m}\right)^{1/2},$$

where $A_j$ and $Q_m$ are the vertical area between the station pairs and the horizontal area of the layer interfaces (neutral density surfaces), respectively. Except for the 2013 realizations at 14.5° N, we set the a priori uncertainties for the reference velocity of the other three realizations to be 0.04 m s$^{-1}$ at the western boundary region, and 0.02 m s$^{-1}$ for the rest of the station pairs following Hernández-Guerra et al. (2014). Since no direct velocity observations are available for these three realizations, the choice of the a priori uncertainty is relatively arbitrary. On the one hand, we have assumed the energetic western boundary currents might have larger uncertainties than flows in the interior ocean. On the other hand, larger uncertainties in the highly dynamical region means higher weighting in the box inverse model, which would give the reference velocity in western boundary region priority to be solved in the inverse model. For the 2013 realization, the a priori uncertainties at the western boundary were estimated based on the variability of the SADCP velocity (Fig. 7, see Sect. 3.3 for details). The diurnal exchanges of volume, salt, and heat are expected to be small in the tropical Atlantic, we set the a priori uncertainty of the diurnal velocity to be in the order of 10$^{-6}$ m s$^{-1}$.

Applying the row and column weightings to Eq. 2, we have

$$(WAE)(E^{-1}x) = Wb,$$

which can be written as

$$A''x' = b',$$

with $A'' = WAE$, $x' = E^{-1}x$, and $b' = Wb$. The weighted system can be solved by using singular value decomposition (SVD) (Wunsch, 1996) by choosing a rank where data residual norms are of O[1 to 2 Sv] (Sloyan and Rintoul, 2001). An error covariance matrix $P$ can be formulated using the Gauss-
Markov method. The a posteriori errors of the solution were estimated as the square root of the diagonal components of $P$, where

$$P = E - EA^T(AEA^T + W)^{-1}AE.$$  \hfill (9)

### 3.5 Sensitivity tests of the inverse model

It is of interest to test how sensitive the inverse results are to the initial conditions and constraints. The 1992 realization at 24.5° N have been used in several previous studies (e.g. Ganachaud, 2003; Lumpkin and Speer, 2003; Hernández-Guerra et al., 2014), we found that the circulation structure and strength is very stable among these studies, even though different hydrographic sections were combined with this realization to build the box inverse models. This can be attributed to the similar steady-state initial condition and constraints applied to the box inverse models. To further quantitatively answer the question, we performed four sensitivity experiments on the 14.5° N section as follows and referred to the box inverse model described in Sect. 3.1-3.4 as the “control run”.

1. **Sensitivity to the meridional Ekman transport.** In this experiment, we used the 1989/1992 box and artificially doubled the Ekman transport at 14.5° N to 17.6 Sv, everything else is identical to the “control run”.

2. **Sensitivity to the reference level.** In this experiment, we shifted the reference level of the 14.5° N section in both boxes from $\gamma_n = 27.82$ to 28.141 kg m$^{-3}$, and kept other conditions the same as in the “control run”. Note that for the 2013 realization, the initial reference velocity was still applied, but re-calculated using the new reference level.

3. **Sensitivity to the initial reference velocity.** In the “control run” of the 2013/2015 box, the reference velocity for the 14.5° N section was estimated using the SADCP/LADCP velocity. In order to test how much the initial reference velocity affects the final transport, we replaced the initial reference velocity at 14.5° N of the 2013/2015 box with 0, and kept everything else identical to the control run.

4. **Sensitivity to hydrographic variability.** To assess the effect of hydrographic variability on the inverse model solution, we conducted 6 experimental runs using the 2013 realizations at the 14.5° N section in combination with six realizations of the 24.5° N section (1992, 1998, 2004, 2010, 2011, and 2015, data available from CCHDO and World Ocean Database). For all six experimental runs, we used
the long-term mean Ekman transport calculated using the monthly NCEP/CFSR wind stress (1979-2010) for both sections and a long-term mean FC transport (31.1±2.4 Sv) at 24.5° N, and kept everything else identical to the control run. In this way, we could examine the stability of the results at 14.5° N against the hydrographic variations at 24.5° N.

### 3.6 Heat and freshwater transport estimation

The heat and freshwater transports through the two sections were estimated using the results from the box inverse model. Note that after the inversion the total volume transport through a section should be quasi zero (except a 0.5-0.8 Sv Bering Strait transport). Therefore, the total heat transport through a section, $H_{\text{sect}}$, can be regarded as a sum of the heat transport associated with the warm northward Ekman transport at the surface, $H_e$, and the much colder southward returning geostrophic flow over the full water column, $H_g$:

$$H_{\text{sect}} = H_e + H_g,$$

where $f$ is the Coriolis parameter; $C_p$ is the specific heat capacity of seawater; $\bar{\theta}_j^\text{surf}$ is the mean in-situ sea surface potential temperature (SST) between the station pair; $\tau_j^f$ is the zonal wind stress from NCEP/CFSR. In this study, we use $g$ and $C_p$ as constants of 9.8 m s$^{-2}$ and 4000 J kg$^{-1}$ K$^{-1}$, respectively. Note that we only use the in-situ SST to calculate the Ekman heat transport, since it has been shown by Fu et al. (2017) that in the tropical Atlantic the Ekman heat transports estimated using in-situ SST and temperature profile data within the Ekman layer only differ marginally. $H_e$ was calculated as

$$H_e = \frac{C_p}{f} \sum_j \bar{\theta}_j^\text{surf} \tau_j^f \Delta x_j,$$  

where $v^\text{abs}_{m,j}$ is the absolute geostrophic velocity in the cell of layer $m$, bounded by station pair $j$, as obtained from the box inverse model; $\bar{\theta}_{m,j}$ is the mean in-situ potential temperature in the same cell of $v^\text{abs}_{m,j}$; $\Delta h_{m,j}$ is the thickness of layer $m$ at station pair $j$. 

$$H_g = \rho C_p \int v^\text{abs}_{m,j} dxdz = \rho C_p \sum_m \sum_j \bar{\theta}_{m,j} v^\text{abs}_{m,j} \Delta x_j \Delta h_{m,j},$$
The freshwater transport through a section was achieved in the sense of salt and mass conservation between the Bering Strait and the corresponding section. It can be expressed as follows (cf. Friedrichs and Hall, 1993, and McDonagh et al., 2015 for details):

\[ F_{\text{sect}} = M_{\text{net}} = M_{\text{BS}} \bar{S}_{\text{BS}} + M_{\text{E}} \bar{S}_{\text{E}} + M_{\text{G}} \bar{S}_{\text{G}} + M_{\text{W}} \bar{S}_{\text{W}}, \]  

(13)

where \( M_{\text{net}} \) is a net barotropic flow through the section; \( M_{\text{BS}} = 0.8 \text{ Sv} \) is the Bering Strait transport, and \( \bar{S}_{\text{BS}} = 32.5 \) is the mean salinity at the Bering Strait; \( < S > \) is the section-areal mean salinity; \( M_{\text{E}}, M_{\text{G}}, \) and \( M_{\text{W}} \) are the Ekman and interior geostrophic, and western boundary volume transport, respectively; \( \bar{S}_{\text{E}} \), \( \bar{S}_{\text{G}} \), and \( \bar{S}_{\text{W}} \) are the Ekman, interior geostrophic, and western boundary transport-averaged salinity. \( \bar{S}_{\text{E}} \) and \( \bar{S}_{\text{G}} \) are defined as follows, \( \bar{S}_{\text{W}} \) is analogue to \( \bar{S}_{\text{G}} \):

\[ \bar{S}_{\text{E}} = \frac{\sum_{i} \sum_{j} \Delta x_{j} \Delta y_{j} \bar{S}^{\text{SSS}}_{\text{E}}}{M_{\text{E}}}, \]  

(14)

and

\[ \bar{S}_{\text{G}} = \frac{\sum_{i} \sum_{j} \sum_{m} \Delta x_{j} \Delta y_{j} \Delta h_{m,j} \bar{S}^{\text{SSS}}_{\text{G}}}{M_{\text{G}}}, \]  

(15)

where \( \bar{S}^{\text{SSS}}_{\text{E}} \) is the mean in-situ salinity in the same cell of \( \bar{S}^{\text{SSS}}_{\text{G}} \); \( \bar{S}^{\text{SSS}}_{\text{W}} \) is the mean in-situ sea surface salinity (SSS) between the station pair \( j \). Note that the western boundary current region at 14.5° N is defined by the western most 6 station pairs, and in the upper 1000 m, while at 24.5° N it is the Florida Strait.

4. Inverse model results

4.1 Adjustments and final transport

The final adjustments to the reference velocity were achieved by solving the box inverse model built with the 14.5° N and 24.5° N sections for the two periods (Fig. 8). For both periods, the largest adjustments appear in the boundary regions, where the a priori uncertainty of the reference velocity is large. For the rest of the sections, the adjustments are small and not significantly different from zero. Similar to the previous inverse model studies, the a posteriori errors have similar magnitude of the a priori uncertainties of the unknowns (Ganachaud, 2003; Hernández-Guerra et al., 2014).
In general, the dianeutral velocity is not significantly different from zero, except in the bottom layer ($\gamma^n > 28.152$ kg m$^{-3}$) of the 2013/2015 period, where a strong upward velocity is observed (Fig. 9). A similar structure of the dianeutral velocity was also achieved by Ganachaud (2003) for the tropical North Atlantic box bounded by 7.5° N and 24.5° N. The densest AABW flows northward in the tropical North Atlantic at the bottom of the western basin, it mixes with the LNADW, resulting in water mass transformation and volume reduction of the AABW. Therefore, it is expected that upwelling occurs in the bottom layer. However, in the 1989/1992 period a downwelling velocity appears at $\gamma^n = 28.152$ kg m$^{-3}$ due to a divergence of the horizontal geostrophic transport in the bottom layer (Fig. 10a). Note that the horizontal area of the surface $\gamma^n = 28.152$ kg m$^{-3}$ is very small since it only exists in the abyssal basin west of the MAR. Therefore, a downwelling velocity in the bottom layer will not change the fact that the AABW as whole upwells, when the upwelling velocity and the much larger horizontal area of the layer surface $\gamma^n = 28.141$ kg m$^{-3}$, which marks the upper boundary of AABW, is taken into account.

Using the adjustments to the reference velocity and the dianeutral velocity, the zonally integrated final transport per layer is calculated, including the Ekman transport in the first layer (Fig. 10). Compared to the initial transport (not shown), clear overturning structures with southward NADW and northward upper, intermediate and bottom waters are achieved for both sections during the respective surveys. The imbalance in layers has been reduced indistinguishable from zero, which implies volume conservation in both boxes after inversion. Note that the imbalance in each layer is calculated after taking into account the meridional and dieneutral transports across the side boundaries and vertical boundaries of that layer. The final transport of water masses can be then calculated by integrating the layer transport over the corresponding layers of a water mass. As summarized in Table 3, for the 14.5° N section, the thermocline water (layer 1-3) has northward transport of $5.4 \pm 1.7$ Sv in 1989, and $2.9 \pm 4.8$ Sv in 2013. The intermediate water (layer 4-6) transport is $4.5 \pm 2.2$ Sv northward in 1989 while $2.8 \pm 1.7$ Sv in 2013, which is weaker in the latter period. Note that due to the higher weighting (small uncertainty in the constraints) of the intermediate water transport at 14.5° N in 2013, the final intermediate water transport in 2013 is very close to the prescribed value of $2.8 \pm 2.1$ Sv. It is important to point out that without this constraint, the final intermediate water transport would be even southward, no matter which reference
level is chosen, and whether the SADCP/LADCP reference velocity is applied or not. However, while being not an adequate solution, it can be seen as a strong indication that the intermediate water transport in 2013 is substantially weaker than that in 1989. Recall the increasing temperatures and salinities in the AAIW layer at 14.5° N between 1989 and 2013, which may be explained by the reduction in the northward supply of fresh and cool AAIW water between the two periods.

In response to the much weaker northward thermocline and intermediate water transport, the UNADW (layer 7–11) transport of $-6.5 \pm 2.7$ Sv in 2013 is also much weaker than that of $-12.0 \pm 3.2$ Sv in 1989 ($\sim$ denotes southward). In comparison, the LNADW (layer 12–15) transport of the periods is very close to each other ($-9.2 \pm 6.1$ Sv in 1989 vs. $-9.6 \pm 6.6$ Sv in 2013). The AABW (layer 16–17) transport is relatively close between the two realizations, with $2.2 \pm 2.3$ Sv in 1989, and $1.4 \pm 2.4$ Sv in 2013, but the northward core of AABW transport shifts to a denser layer (from layer 16 to 17) between 1989 and 2013.

At 24.5° N, in contrast to the 14.5° N section, the circulation structure is relatively stable between 1992 and 2015 (Fig. 11b). The transport of thermocline water (layer 1–4) excluding the FC transport is $-18.0 \pm 1.0$ Sv in 1992, while it is $-20.1 \pm 1.2$ Sv in 2015, which is stronger southward. The northward intermediate water (layer 5–6) transport is also slightly weaker in 2015 ($3.1 \pm 1.2$ Sv) than in 1992 ($4.0 \pm 1.2$ Sv). A stronger southward transport in the thermocline water and a weaker northward transport in the intermediate water indicate together a weaker northward transport in the upper ocean in the more recent period than in the former period. As a result, the southward NADW transport in 2015 are also weaker than that in 1992 by about $3.6$ Sv. The AABW transport is also slightly weaker in the more recent period ($2.1 \pm 2.5$ Sv in 1992 vs. $1.2 \pm 2.6$ Sv in 2015).

In order to compare the intensity of the AMOC between the different periods, an overturning stream function of each realization was calculated by cumulatively integrating the layer transport from the surface to the bottom (Fig. 11). The AMOC strength is defined as the maximum northward transport of the overturning stream function. At 14.5° N, the AMOC strength is $19.2 \pm 2.7$ Sv in 1989, and $14.3 \pm 2.2$ Sv in 2013. At 24.5° N, the AMOC strength is $19.6 \pm 1.6$ Sv in 1992, and $17.1 \pm 1.6$ Sv in 2015. It appears that at both latitudes the AMOC is weaker during 2013/2015 than during 1989/1992, but the weakening is not significant. As described above, at both latitudes, we see a reduction of northward thermocline
and intermediate water between the two periods, which is compensated by a decrease of the southward UNADW transport. It is worth to note that, the 1992 realization at 24.5° N has been used by many global and regional inverse studies (Ganachaud, 2003; Lumpkin and Speer, 2003; Hernández-Guerra et al., 2014). Despite the fact that various other sections are combined with this realization to perform box inverse models, the vertical structure of the circulation and the transport strength are strikingly similar for this realization. All these studies have imposed a more or less time-mean Ekman transport and FC transport, as well as similar a priori errors (weightings) to the box inverse model. This indicates that given a steady-state initial condition, stable inverse results may be achieved, though the baroclinic structures and measurement errors (e.g. due to internal wave field) of the combined section are very different.

4.2 Horizontal circulation pattern

The absolute geostrophic velocity sections are shown in Fig. 12. In the upper 1000 m at 14.5° N, intensified northward currents are confined at the western boundary. In 1989, the two branches of the western boundary current with nearly equal amount of transport are located within a narrow channel and along the continental slope. A very weak southward flow separates the two branches in between. The western boundary current transport at 14.5° N in 1989, estimated by integrating the final total velocity from the western boundary to the eastern extent (58.30° W) of the northward current in the upper 1000 m, is 27.6±3.2 Sv, which is somewhat larger than an estimate of 18 to 24 Sv by Klein et al. (1995). However, the difference does not come surprisingly, since their result was obtained by using a seasonal Ekman transport of 15.94 Sv, which is two times higher than the annual climatological value of 7.9±3.5 Sv at this latitude estimated by Fu et al. (2017). As Ekman transport and western boundary current are the dominant northward components of the AMOC in the tropics, such a strong Ekman transport would result in, to the lowest order of volume conservation, a weaker western boundary current. The impact of a large Ekman transport on the transport results is discussed as a sensitivity study later.

In 2013, the western boundary current was not evenly distributed into two branches; instead, it was much more confined in the narrow channel, and amounted to 27.5±5.4 Sv. This value compares favorably with a transport of 25.3±9.2 Sv estimated using the LADCP cross-section velocity and errors
within the channel. Along the continental slope it was much weaker, and almost replaced by a much stronger southward flow compared to that in 1989.

At 24.5° N, the western boundary current system is primarily the FC with a transport of 31.2±0.3 Sv and 31.2±0.9 Sv in 1992 and 2015, respectively. These values are not significantly different from the constrained values (cf. Table 2), and are consistent with a long-term mean value of 31.1±2.4 estimated by Atkinson et al. (2010). Fig. 13 shows the vertical sections of the meridional geostrophic velocity in the Florida Straits. In both realizations, the structure of the Florida Current is consistent with previous observations (i.e., Leaman et al., 1987). It is very clear that the maximum northward velocity core is located near the western boundary of the Florida Straits. The maximum velocity in 1992 is larger than 2 m s⁻¹, and in 2015 it is about 1.95 m s⁻¹. Note that the measurements within the Florida Straits were carried out near 26° N in 1992 and near 27° N in 2015, and that the reference velocity obtained from the box inverse model are very uniform through the Straits for both periods. Therefore, the observed difference in the Florida Current structure between the two periods may be related to the different topography and hydrographic structure.

Along the western boundary at greater depth, two southward velocity cores can be seen in all sections over a neutral density range of 27.82 to 28.072 kg m⁻³ and 28.072 to 28.141 kg m⁻³, respectively (Fig. 12), which are associated with the DWBC. The high oxygen concentration found in the deep western boundary region roughly coincides with the depth of the DWBC velocity cores (Fig 5). For the 2013 realization at 14.5° N, the dual-core structure mentioned above is also evident in the oxygen section with oxygen concentration larger than 260 µmol kg⁻¹. The relatively lower oxygen concentration at about 3000 m between the two cores also coincides with a minimum southward flow in the corresponding neutral density layer (28.044<γ_n<28.072 kg m⁻³, Fig. 10b). This structure is consistent with the vertical structure of the NADW transport observed in the western basin by the MOVE at 16° N (Send et al., 2011). Send et al. (2011) showed that the annual mean NADW transport has two southward maxima located at 2000 m and 4000 m, corresponding to the LSW and DSOW, respectively, and a minimum in between centered at 3000 m, corresponding to the ISOW. The high oxygen concentration in this area also implies the presence of relatively recently formed waters of northern origin (LSW,
ISOW, and DSOW), which is also evident from higher transient tracer concentrations (e.g. Chlorofluorocarbons, CFC; Molinari et al., 1992).

In order to calculate the DWBC transport, an eastern boundary of the DWBC must be defined for integration purpose. This boundary is defined by the eastward extent of the southward velocity in the NADW layers (27.82 < \( \gamma_n < 28.141 \) kg m\(^{-3}\)) in the western basin. At 14.5° N, we used 51° W for both realizations as the eastern boundary of the DWBC, which coincides with the high-CFC cores measured during the 1989 realizations (cf. Fig. 3 in Molinari et al., 1992), and with the high-oxygen cores measured during the 2013 realizations (Fig. 5c), respectively. Note that this definition includes the northward recirculation branches near the continental slope. The resulting DWBC transport is \(-22.1 \pm 9.6\) Sv in 1989 and \(-21.3 \pm 8.0\) Sv in 2013, respectively. For the 24.5° N section, we used 72° W as the eastern boundary of the DWBC for both realizations, resulting in a DWBC transport of \(-26.6 \pm 4.6\) Sv in 1992 and \(-26.5 \pm 4.0\) Sv in 2015, respectively.

The DWBC transport estimates at 14.5° N compare favorably with an estimate of 25 Sv at 10° N in the Atlantic by Speer and McCartney (1991), and a mean DWBC transport of 26.0 ± 8.0 Sv in the tropical North Atlantic by Molinari et al. (1992), which was calculated by using repeated cruise sections between 14.5° N and the equator. Friedrichs and Hall (1993) have shown that at 8° N in the Atlantic, 27 Sv were transported southward within the DWBC along the continental slope, which was accompanied by a northward recirculation of 16 Sv primarily along the western flank of the MAR. They further schematically showed that the whole tropical North Atlantic adopted such a circulation pattern. However, in this study, at 14.5° N, northward recirculation occurred at the western flank of the MAR, but also near the continental slope to the east of the southward cores of the DWBC. For the 1989 realization, the recirculation near the continental slope accounts to \(-12.0\) Sv, while that at the western flank of MAR is \(-13.1\) Sv. For the 2013 realization, the recirculation near the continental slope is \(-16.5\) Sv, while northward velocity is found in a large area over the MAR, which is likely a compensating flow of the strong southward velocity with similar strength between 42 and 35° W (Fig. 12). Due to the limitation of the maximum operation depth (6000 m), the LADCP was not operated in this area. But a strong southward flow is still evident in the SADCP sections in the upper 1200 m (not shown).
4.3 Sensitivity of the box inverse model

As described in Sect 3.5, three sensitivity experiments were conducted to test the sensitivity of the box inverse model to the different initial conditions and constraints. The results of the sensitivity tests are presented here and compared with the results presented in Sect. 4.1 and 4.2 (referred to as “Control run”).

4.3.1 Response to meridional Ekman transport

This experiment shows that the upper ocean geostrophic transport has an immediate response to the change in the Ekman transport at the same section. When the Ekman transport at 14.5° N in the 1989/92 box is artificially doubled (from 8.8 Sv in the control run to 17.6 Sv in the experimental run), the thermocline and intermediate water transport strongly decreases, from $5.4 \pm 1.7$ Sv and $4.5 \pm 2.2$ Sv (in the control run) to $-0.6 \pm 1.7$ Sv and $1.5 \pm 2.2$ Sv, respectively. The NADW and AABW transport as well as the overturning strength change only marginally. The transport at 24.5° N is also insensitive to the change in the Ekman transport at 14.5° N. This may explain the very small (even southward) AAIW transport ($-0.7$ Sv) in the seasonal case of Klein et al. (1995), who applied an extremely large Ekman transport (15.94 Sv) at 14.5° N to a box inverse model combining the 1989 realization at 14.5° N and 1957 realization at 8° N.

4.3.2 Sensitivity to reference level

This experiment shows that when no additional constraints are applied, it is very important to choose a proper initial reference level, in order to obtain a reasonable DWBC transport. For the 1989 realization at 14.5° N, the thermocline and intermediate layer transports are insensitive to the change of the reference level. Combined with the same Ekman transport applied in the surface layer, they result in a nearly identical AMOC strength. However, in the deep and bottom water layer, especially in the DWBC region, the transport is very different. Although the total NADW transport does not decrease dramatically, the DWBC transport changes from $-21.5 \pm 9.6$ (southward) to $6.5 \pm 9.6$ (northward). The DWBC is defined as the transport between $\gamma = \gamma_0 = 27.82$ and $28.141$ kg m$^{-3}$, west of 51° W. The dramatic reverse of the DWBC transport indicates that the main southward NAD transport occurs near the...
MAR and in the eastern basin instead of within the DWBC. Additionally, the AABW transport also strongly decreased from 2.5±2.3 Sv to -0.3±2.3 Sv. Based on the results of this sensitivity experiment, we finally chose $\gamma_n = 27.82$ kg m$^{-3}$ as the reference level for the 1989 realization, which provides a more canonical circulation pattern. For the 2013 realization, due to the fact that the initial reference velocity is constrained using values retrieved from the SADCP/LADCP, the inverse solution is insensitive to the choice of the reference level.

4.3.2 Sensitivity to reference velocity

This experiment shows that the circulation pattern is sensitive to the reference velocity, but the AMOC strength is not. Removing the initial reference velocity of the 2013 realization at 14.5° N would decrease the UNADW transport from 6.5±2.6 Sv to 2.7±2.6 Sv, while increase the UNADW transport from -9.6±6.6 Sv to -13.2±6.6 Sv. As shown in Fig. 7, the initial reference velocity (2013 at 14.5° N) directly along the continental slope (station pair 6 to 8) is southward, while slightly away from the slope (station pair 9 to 13) it is mainly northward. Removing the reference velocity, would weaken the upper core of the DWBC, but at the same time weaken the northward recirculation alongside the DWBC cores. Such a change in the DWBC region is not surprising, provided the least-square nature of the box inverse method, it would always minimize the size of the correction to the initial reference velocity (McIntosh and Rintoul, 1997). Therefore, the experimental run can hardly reproduce the magnitude of certain circulation elements (e.g. DWBC) defined by the reference velocity that is far away from 0. Besides, initializing the reference velocity using known (observed) velocity field is common in box inverse studies (e.g. Tsubouchi et al. 2012), and we believe it provides us a robust circulation pattern in this study.

4.3.4 Effect of hydrographic variability

The results show that the hydrographic variation at one section does affect the circulation structure and strength at the other section. Taking the AMOC strength as an indicator, in the six experimental runs combining the 2013 realization of 14.5° N, the AMOC strength at 14.5° N varies between 11.3±3.7 Sv (2013/2004 run) and 16.7±3.7 Sv (2013/1992 run) with a mean value of 14.3 Sv. These results are not
significantly different from that of the control run (14.3±5.2 Sv). Since all the constraints and initial conditions were given using the long-term mean value and kept unchanged among the runs, the only candidate for the change is the different baroclinic and horizontal shear structures that are related to interannual to decadal variability or/and the measured eddy and internal wave field. Note that among the six experimental runs, the AMOC strength at 14.5° N from the combinations of 2013/2010, 2013/2011, and 2013/2015 is very stable (15.3±3.3 Sv, 15.2±3.6 Sv, and 14.5±3.7 Sv, respectively). This is an indication of the importance to perform a box inverse model using sections occupied in the nearby years.

### 4.4 Heat and freshwater transports

At 14.5° N, we estimated the heat transport through the section as northward 1.06±0.14 PW (1 PW = $10^{15}$ Watt) in 1989 and 1.06±0.15 PW in 2013. Despite the fact that the strength of AMOC is weaker in 2013 than in 1989, the heat transport in 2013 is almost the same as in 1989. This can be attributed to the source of the transport changes and to the higher mixed layer temperature (a mean offset of 1.60 °C in the upper 50 m) during the occupation in May 2013 than in February 1989. As shown in Fig. 11, the reduction of AMOC strength occurs mainly in the lower thermocline and intermediate water transport (layer 3-5), which carries much less heat northward compared with the surface water transport (layer 1-2). The surface water transport is even stronger in 2013 than in 1989. Compared with the estimates of 1.22 PW (annual case) or 1.37 PW (seasonal case) by Klein et al. (1995), our heat transport estimate for the 1989 realization is small. However, in the sensitivity test (Sect. 4.3.1), corresponding to a 17.6 Sv Ekman transport, the heat transport amounts up to 1.50±0.14 PW, which explains the large heat transports in Klein et al. (1995). Fu et al. (2017) showed that in the tropical Atlantic the SST can be used to represent the transport-weighted mean temperature in the Ekman layer, and that the uncertainty of the Ekman volume transport dominates the uncertainty of the associated heat transport. Combining their conclusion with the results of the sensitivity test to the Ekman transport, it is suggested that the total heat transport across 14.5° N is sensitive to the Ekman volume transport. The heat transport through the 24.5° N section is estimated as northward 1.39±0.10 PW in 1992 and 1.09±0.11 PW in 2015. The strong decrease of the heat transport between the two years reflects the...
reduction of the northward transport in the surface layers (layer 1-4, Fig. 11). The heat transport at 24.5° N has been estimated for several times in previous studies, especially for the 1992 realization; for instance, Ganachaud and Wunsch (2003) calculated a heat transport of 1.27±0.15 PW in 1992. Hernández-Guerra et al. (2014) estimated the heat transport as 1.4±0.1 PW in 1992 and 1.2±0.1 PW in 2011. All the above listed heat flux estimates align with a RAPID array-based estimate of 1.25±0.36 PW (mean ± standard deviation) by Johns et al. (2011) at 26.5° N.

The freshwater transport across the 24.5° N section is estimated as -1.25±0.20 and -0.97±0.20 Sv in 1992 and 2015, respectively. For the 1992 realization, the estimate here agrees well with that of -1.23 Sv by Rosón et al. (2003) and -1.16 Sv by McDonagh et al. (2015). The estimate in 2015 falls in the range of -0.93 to -1.26 Sv based on hydrographic data or -1.17±0.20 Sv based on RAPID array data (see McDonagh et al., 2015, for a summary). At 14.5° N the freshwater transport was -1.02±0.15 and -0.99±0.22 Sv in 1989 and 2013, respectively. This is the first freshwater transport estimation at 14.5° N based on hydrographic data; compared to the estimates based on surface freshwater transport (i.e., integrating the evaporation, precipitation and river runoff from a northern latitude with initial condition; Wijffels et al., 1992), it is somewhat larger. However, given a net surface freshwater loss of about 0.3 Sv between 24.5° N and 14.5° N estimated using HOAPS data and -1.17±0.20 Sv as the initial condition at 24.5° N, the estimates at 14.5° N are still within the uncertainty range.

Note that the uncertainties of the freshwater transports were estimated following Friedrichs and Hall (1993) as the amount of freshwater transport change due to an assumed salinity uncertainty of 0.2 psu in the western boundary at each section. This assumption is based on the fact that the freshwater transport is very sensitive to the transport-weighted salinity in the western boundary (\(S_w\)) rather than any transport component in Eq. 13. At both latitudes, an uncertainty of ±0.2 psu in \(S_w\) leads to a freshwater transport uncertainty of 0.1-0.2 Sv, while about 10 Sv change in \(M_{sw}\) would be required to obtain a freshwater transport change of the same amount.

5 Comparison with the GECCO2 state estimate, RAPID and MOVE analysis data

The inverse results for the two sections during two different periods have shown overturning structure of comparable strength with previous studies in similar regions. In order to validate the inverse solution,
here we first compare the vertical structure obtained from the inverse model with that from the RAPID array data. At 24.5° N, the RAPID array data provide estimates of meridional transports across the section from 2004 to 2017 (Smeed et al., 2017). Here, we calculated the meridional overturning stream function using the absolute velocity field of the 2015 realization obtained from the inverse model, and compared it with the mean meridional overturning stream function of the RAPID array in 2015. Note that the transport for the RAPID array is calculated based on depth levels. Therefore, for comparison, the overturning transport of the inverse results is also calculated as a function of depth. As shown in Fig. 1, the overturning stream function from the inverse method and the RAPID array are overall consistent with each other, with a very similar overturning (17.1±1.6 Sv for the inverse method, 17.0±4.4 Sv for the RAPID array). The overturning strength is defined as the maximum northward transport in the meridional overturning stream function, typically at about 1000 m. The uncertainty of the RAPID array is given by the standard deviation of the RAPID time series. Note that the definition of water masses for the RAPID array is based on depth levels (thermocline water 0-800 m, intermediate water 800-1100 m, UNADW 1100-3000 m, LNADW 3000-5000 m, AABW >5000 m), while for the inverse model, the water masses are defined by the neutral density surfaces. To best represent the depth definition of water masses, we have chosen the neutral density surfaces of 27.38, 27.82, 28.072, 28.1295 kg m$^{-3}$ as the boundaries between these water masses. Note that here the boundary between the LNADW and AABW is different from the previous definition only for comparison purpose. The thermocline water transport without the Florida current is -20.7±1.2 Sv for the inverse method, and -19.1±3.3 Sv for the RAPID array. The intermediate water transport of the inverse method (1.5±1.2 Sv) is slightly stronger than the RAPID (0.6±0.6 Sv). The largest difference in the overturning stream function between the two estimates occurs at about 3000 m, the transport approaches to each other gradually between 3000 and 5000 m. This indicates that in comparison to the RAPID array, the inverse model underestimates the UNADW transport (-9.6±1.9 Sv for the inverse method, -11.6±2.5 Sv for RAPID), and overestimates the LNADW transport (-9.3±5.5 Sv vs -6.3±2.9 Sv), but the total transport of the NADW appears to be very close (-18.2±5.4 Sv vs -17.9±4.0 Sv). The AABW transport is 1.2±2.6 Sv for the inverse method, and 0.9±0.6 Sv for RAPID array, also not significantly different from each
other. This comparison shows that provided with time-averaged (annual mean) constraints, the box inverse model is able to reasonably reproduce the observed (RAPID) AMOC strength and structure. The inverse solution does not show any significant weakening of the AMOC at both latitudes. In order to verify this conclusion, we compare the AMOC strength calculated from the inverse solution with that of the GECCO2 ocean state estimate (Jan 1985 to Dec 2014), the RAPID array data (Apr 2004 to Feb 2017), and the MOVE array data (Feb 2000 to Feb 2016) (Fig. 15). Köhl (2015) showed that the annual mean overturning stream function calculated from GECCO2 agreed very well with that from the RAPID array data in the upper 2500 m. In other words, GECCO2 represents the observed AMOC strength very well, as can be seen from the overlapping period between the assimilated (GECCO2) and observed (RAPID) AMOC strength time series (Fig. 15a). The overturning strengths of GECCO2 at both latitudes exhibit a strong seasonal cycle, with the maximum transport in boreal winter, and minimum in boreal summer. The seasonal difference of the strength can reach up to 15 Sv. The 20-month low-passed AMOC strength of GECCO2 also reveals interannual variability at both latitudes. For instance, a continuous decline of the AMOC strength between 2008 and 2012 is captured by GECCO2 at both latitudes, which is also observed by the RAPID array. The good agreement between the RAPID and GECCO2 AMOC strength at 24.5° N within the common period has lent us confidence to use the GECCO2 data to validate the inverse results at the other section and back to the period of 1989/1992. At the two latitudes, the AMOC strength calculated from the inverse method agrees with the GECCO2/RAPID AMOC strength in the respective years within error bars. The GECCO2 AMOC strength time series does not show any trend at both latitudes over the presented period either. Therefore, we may conclude that the AMOC in the tropical North Atlantic has not significantly weakened between the two periods, and that the observed differences in the AMOC between the respective realizations are more likely due to short-term variability of the AMOC. The 120-day low-pass filtered MOVE array transport time series at 16° N is shown in Fig 14b, as a representation and update of Fig. 2 in Send et al. (2011). The MOVE array is composed of a current meter mooring at the western boundary, and two end-point geostrophic moorings at each end of the western basin at 16° N, which measures the DWBC and interior geostrophic transport between 1200 and 4950 m in the western basin. An assumption behind this mooring configuration is that the...
southward flow in the NADW layer in the western basin should represent (almost) entirely the southward return limb of the AMOC, thus the AMOC intensity (Send et al., 2011). Note that the sign of the MOVE transport in Fig. 15b is reversed for comparison purpose. In contrast to the good agreement between the AMOC strength calculations from the inverse method, GECCO2, and RAPID at 24.5° N, the AMOC strength from the MOVE array does not seem to align with that of the inverse method and GECCO2 at 14.5° N (Fig. 15b). Although the MOVE transport also shows seasonal to interannual variability up to 20 Sv, the magnitude of the MOVE transport (24.1±4.1 Sv) is generally larger than that of GECCO2 at 14.5° N (15.8±3.4 Sv) throughout most of the overlapping period. Additionally, the MOVE transport shows a significant increasing trend of 8.4±5.6 Sv decade⁻¹ since April 2004 (Baringer et al., 2015; by using data from Apr 2004 to Oct 2013 and 95% confidence interval), whilst the RAPID transport has a significant decreasing trend of -4.1±3.2 Sv decade⁻¹ over the same period. Extending the data to date, RAPID time series does not show a significant trend on 95% confidence interval, while at 16° N the trend remains similar at 8.2 Sv decade⁻¹ (both using two-sided t-test on 95% confidence interval). Since the NADW originates from the subpolar North Atlantic, and is transported southward, any long-term signal observed in the RAPID section is expected to appear later in the MOVE section. Assuming the same transit speed as the water traveling from the Labrador Sea to 26° N (9 years, van Sebille et al., 2011), it would take 2-3 years for the same water to reach 16° N (Smeed et al., 2014). However, this does not seem to be the case when comparing results from these two observation systems. Speculations can be made to explain these discrepancies, such as whether the assumption behind the MOVE array that the NADW through the western basin is representative of the whole southward return limb of the AMOC, or whether the reference level of no motion vary with time, etc., are fulfilled. The geostrophic velocity sections at 14.5° N (Fig. 12a, c) show northward recirculation over the MAR, which may not be fully resolved by the eastern most mooring of the MOVE array. However, it is impossible to verify whether it is a standing or transient feature based on the available data.
In this study, hydrographic data from trans-Atlantic sections at 14.5° N occupied in 1989 and 2013, and at 24.5° N occupied in 1992 and 2015, are presented. Through comparison between the earlier realizations (1989, 1992) and the more recent realizations (2013, 2015) at the respective latitude, we have shown property changes of water masses over time. At 14.5° N, basin-wide warming and salinification of AAIW on neutral surfaces is observed in the $\gamma_n$ range between 27.38 to 27.82 kg m$^{-3}$ (Fig. 3e and 4e). Previous studies have also shown that at 7.5° N in the Atlantic, warming occurred in the intermediate layer (500-2000 m) through comparison of hydrographic data measured in 1957, 1993, and 2000 (Arhan et al., 1998; Sarafanov et al., 2007, 2008), and a significant decrease of the northward AAIW transport at this latitude (Hernández-Guerra et al., 2014). Schmidtko and Johnson (2012) further showed warming and salinification trends of the AAIW core in the tropical North Atlantic since the mid-1970s. They attributed the trends in the Atlantic to an increase in winter SST in the AAIW formation region, and to a strengthened Agulhas leakage associated with a low SAM during some periods of the 20th century, which imports more warmer and saltier Indian Ocean water to the Atlantic (Beal et al., 2011).

The density of the densest AABW at both latitudes decreased over the studied period, at 14.5° N from 28.1686 kg m$^{-3}$ in 1989 to 28.1623 kg m$^{-3}$ in 2013, and at 24.5° N from 28.1596 kg m$^{-3}$ in 1992 to 28.1540 kg m$^{-3}$ in 2015. This implies that the denser AABW observed previously in the western basin has depleted, and that the lighter AABW type is now present, leading to a downward displacement of the isoneutrals. As a result, differencing $\theta$ on pressure levels, we observed an overall warming in the AABW layers with $\gamma_n$ larger than 28.141 kg m$^{-3}$ at 24.5° N, whilst at 14.5° N a warming at the bottom of the continental slope (west of 55° W, and $\gamma_n$>28.141 kg m$^{-3}$). This is consistent with the previous studies by Johnson et al. (2008), who illustrated the warming of AABW in the North Atlantic using repeated zonal and meridional sections; and by Herrford et al. (2017), who showed that in the equatorial region, the temperature of the coldest AABW increased since the early 1990s. Additionally, freshening of the entire NADW between 2013/2015 and 1989/1992 is observed at both sections. This is consistent with observations in the NADW formation regions, showing the source water of the NADW has been freshening since several decades (Dickson et al., 2002), and is a supplement to the observations
showing that the freshening signal of the NADW has reached the tropical South Atlantic (Hummels et al., 2015).

By applying a box inverse model to the trans-Atlantic sections at 14.5° N and 24.5° N for a 1989/1992 period and a 2013/2015 period, the meridional overturning transport and the horizontal circulation pattern at the two latitudes and in different periods are obtained. The zonally integrated meridional transports per water mass for different realizations at the two latitudes are summarized in Table 3. Corresponding to the warming and salinification of the AAIW, we observed that at 14.5° N, the northward intermediate layer transport in 2013 was considerably weaker than in 1989 (Fig. 10 and 11a).

We estimated that the western boundary current transport in 1989 amounted to 27.6±3.2 Sv, partitioned nearly equally into two branches confined in the narrow channel and along the continental slope. In 2013, the western boundary transport amounted to 27.5±5.4 Sv, but was confined almost entirely within the channel, which is also supported by the LADCP data measured during the 2013 realization. Compared to an estimate of 18-24 Sv by Klein et al. (1995), our western boundary current in both realizations is strong, but we believe that their results are biased by an extremely large Ekman transport (15.94 Sv) used in their application of a box inverse model. The Lesser Antilles is located to the west of the 14.5° N section (Fig. 1), connecting the Caribbean Sea with the Atlantic. Recent observations combined with a model study suggest that a total flow of 17-19 Sv passes through the Lesser Antilles into the Caribbean Sea (Kirchner et al., 2008), implying that the western boundary current across the 14.5° N section must recirculate southward across the section in the east, as occurs in both realizations (Fig. 12a, b).

The DWBC transport at 14.5° N was -22.1±9.6 Sv in 1989 and -21.3±8.0 Sv in 2013, which is in agreement with the previous estimates ranging from -16 to -27 Sv in the tropical North Atlantic (Speer and McCartney, 1991; Molinari et al., 1992; Friedrichs and Hall, 1993). Different from Friedrichs and Hall (1993), we found that the northward recirculation occurred both at the western flank of the MAR, and directly to the east of the southward core along the continental slope. At 24.5° N, the DWBC transport was -26.6±4.6 Sv in 1992 and -26.5±4.1 Sv in 2015, which are ultimately close to the a priori constraint of -26.5±13.5 Sv, and agree with the estimates of -24.2 Sv, -26.5 Sv, and -32±16 Sv by Bryden et al. (2005), Johns et al. (2008), and Meinen et al. (2013), respectively.
The inverse solution does not show a significantly weaker AMOC in 2013/2015 than in 1989/1992 at both latitudes, which is confirmed through comparison between the inverse solution, the RAPID, MOVE and GECCO2 data. The observed difference in the AMOC between 1989/1992 and 2013/2015 should be due to short-term variability rather than a long-term weakening trend of the AMOC, as indicated by the GECCO2 and RAPID time series.

During 2013/2015, the inverse solution shows a weaker northward thermocline and intermediate water transport at both 14.5° N and 24.5° N, which is compensated by a correspondingly weaker southward UNADW transport. Regarding the deep-water formation as a primary driver of the AMOC, the long-term variability observed at lower latitudes might be related to changes in the export rate of deep waters in the subpolar North Atlantic. The variability of the NADW transport at 16° N estimated from the MOVE array was attributed to interannual variability in LSW transport (Send et al., 2011). However, studies based on the RAPID array at 26° N show that the variability of the AMOC is more related to the changes in the LNADW transport rather than the UNADW (McCarthy et al., 2012; Smeed et al., 2014), contrary to the MOVE-based conclusion. The discrepancy in the source of the AMOC variability between the two latitudes is still unclear and needs further studies. Observations show that the LNADW source water transport, originating from the Nordic Seas, is very stable (Hansen et al., 2016; Jochumsen et al., 2017). Observations also suggest that the formation of Labrador Sea Water, which contribute to the UNADW, is not linked to the DWBC transport in the Labrador Sea (Zantopp et al., 2017). Consequently, variability in NADW formation is not expected to correlate well with the generation and propagation of transport signals in the DWBC.

We also estimated the heat transport through the 14.5° N section as 1.06±0.14 PW in 1989 and 1.06±0.15 PW. Compared to the estimates of 1.22 or 1.37 PW (annual or seasonal case) using the 1989 realization at 14.5° N by Klein et al. (1995), our estimates are considerably smaller. This is mainly due to the anomalously strong Ekman transport applied in their version of box inverse model, as demonstrated in the sensitivity test of the box inverse model to the Ekman transport (cf. Sect. 4.3.1). At 24.5° N, the heat transport was 1.39±0.10 PW in 1992 and 1.49±0.11 PW in 2015, which are consistent with the previous estimates using hydrographic data ranging between 1.2 and 1.4 PW (e.g. Ganachaud...
and Wunsch, 2003; Hernández-Guerra et al., 2014), and estimates based on the RAPID array of
1.25±0.36 PW (Johns et al., 2011).

As a closing note, we would like to raise some cautions when interpreting the box inverse model results, although we did not claim any long-term change of the AMOC at 14.5° N and 24.5° N. We argued that based on a number of box inverse studies, a time-averaged circulation can be achieved by applying time-averaged initial conditions to the box inverse model (Ganachaud and Wunsch, 2000; Ganachaud, 2003; Lumpkin and Speer, 2003; Hernández-Guerra et al., 2014). However, it is still not possible to rule out any potential influence of the temporal variability of the AMOC captured by the non-synoptic surveys on the inverse results; after all the two inverse boxes in this study were built on sections occupied in different seasons and different years. Intense seasonality of the tropical current system and the tropical/subtropical cells would impact the western boundary current and the interior meridional transport. The interannual variability in the deep-water formation region would also affect the returning limb of the AMOC. Through a sensitivity test, it is suggested that the hydrographic variations at one section affect the circulation at the other section, and that it is maybe important to perform a box inverse model combining sections occupied in nearby years (cf. Sect. 4.3.3 for details). Moreover, even though the AMOC has not significantly weakened so far, we do observe continuous changes of water mass properties. This is notable since model simulations suggest that accumulated changes of water mass properties may eventually trigger changes in the circulation. Therefore, continuous efforts on hydrographic observations must be spent in order to closely monitor the changes of water mass properties, as well as circulations.

7 Data availability

the 14.5° N section are available at https://www.nodc.noaa.gov/OC5/WOD/pr_wod.html. The hydrographic and velocity measurements during cruise M09, M96 and M97 will be available through PANGEA at https://doi.org/10.1594/PANGAEA.870516.

8 Acknowledgements

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Ganachaud, A., Wunsch, C., Marotzke, J. and Toole, J.: Meridional overturning and large-scale


Lumpkin, R. and Speer, K.: Large-Scale Vertical and Horizontal Circulation in the North Atlantic


Table 1. Neutral density surfaces (\(\gamma_n \text{ kg m}^{-3}\)) that separate the layers in the box inverse model. The water masses are labeled to the approximately corresponding layers.

<table>
<thead>
<tr>
<th>Layer</th>
<th>Lower surface ((\gamma_n \text{ kg m}^{-3}))</th>
<th>Water mass</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>26.44</td>
<td>Surface water</td>
</tr>
<tr>
<td>2</td>
<td>26.85</td>
<td></td>
</tr>
<tr>
<td>3</td>
<td>27.162</td>
<td>SACW/NACW</td>
</tr>
<tr>
<td>4</td>
<td>27.38</td>
<td></td>
</tr>
<tr>
<td>5</td>
<td>27.62</td>
<td></td>
</tr>
<tr>
<td>6</td>
<td>27.82</td>
<td>AAIW/MW</td>
</tr>
<tr>
<td>7</td>
<td>27.922</td>
<td></td>
</tr>
<tr>
<td>8</td>
<td>27.975</td>
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</tr>
<tr>
<td>9</td>
<td>28.008</td>
<td>UNADW</td>
</tr>
<tr>
<td>10</td>
<td>28.044</td>
<td></td>
</tr>
<tr>
<td>11</td>
<td>28.072</td>
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<td>12</td>
<td>28.0986</td>
<td></td>
</tr>
<tr>
<td>13</td>
<td>28.11</td>
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<tr>
<td>14</td>
<td>28.1295</td>
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</tr>
<tr>
<td>15</td>
<td>28.141</td>
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<tr>
<td>16</td>
<td>28.154</td>
<td>AABW</td>
</tr>
<tr>
<td>17</td>
<td>Bottom</td>
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Table 2. Constraints for the box inverse model and the final adjusted transport after inversion. Note that the box inverse model does not adjust the meridional Ekman transport, which is prescribed using the annual zonal wind stress during the calendar year of the cruise. The unit of the transport is Sv. Southward transport is given with “−”.

<table>
<thead>
<tr>
<th></th>
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<th></th>
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<tr>
<td>24.5° N</td>
<td></td>
<td></td>
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<td></td>
<td></td>
</tr>
<tr>
<td>Ekman transport</td>
<td>Full section</td>
<td>4.5</td>
<td>−</td>
<td>4.6</td>
<td>−</td>
</tr>
<tr>
<td>Florida Current</td>
<td>Florida strait</td>
<td>All</td>
<td>31.3±1.1</td>
<td>31.2±0.3</td>
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<tr>
<td>Bering strait</td>
<td>Full section</td>
<td>All</td>
<td>-0.8±0.6</td>
<td>-0.9±0.3</td>
<td>-0.8±0.6</td>
</tr>
<tr>
<td>DWBC</td>
<td>77°14' W</td>
<td>7:14</td>
<td>-26.5±13.6</td>
<td>-26.5±14.6</td>
<td>-26.5±13.6</td>
</tr>
<tr>
<td>14.5° N</td>
<td></td>
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<tr>
<td>Ekman transport</td>
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<td>−</td>
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<tr>
<td>Intermediate Water</td>
<td>Full section</td>
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<td>Not applied</td>
<td>4.5±2.2</td>
<td>2.8±2.1</td>
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</table>
Table 3. The final adjusted transport (Sv) of water masses, DWBC, and AMOC intensity at the two sections in the respective years. Southward transport is marked with “–”. The values in the brackets at 24.5° N denote the transport results including the Florida current transport in the corresponding water mass layers.

<table>
<thead>
<tr>
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<th>14.5° N</th>
<th>24.5° N (including Florida)</th>
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<tbody>
<tr>
<td></td>
<td>1989</td>
<td>2013</td>
</tr>
<tr>
<td></td>
<td>1992</td>
<td>2015</td>
</tr>
<tr>
<td>Thermocline</td>
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<td>2.9±4.8</td>
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<tr>
<td></td>
<td>-18.0±1.1</td>
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<tr>
<td></td>
<td>-20.7±1.2</td>
<td>9.5±1.2</td>
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<tr>
<td>Intermediate</td>
<td>4.5±2.2</td>
<td>2.8±1.7</td>
</tr>
<tr>
<td></td>
<td>1.5±1.2</td>
<td>4.0±1.2</td>
</tr>
<tr>
<td></td>
<td>1.5±1.2</td>
<td>3.0±1.2</td>
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<tr>
<td>UNADW</td>
<td>-12.0±3.2</td>
<td>-6.2±2.7</td>
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<tr>
<td></td>
<td>-11.9±1.7</td>
<td>-9.6±1.9</td>
</tr>
<tr>
<td>LNADW</td>
<td>-9.7±6.1</td>
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<td></td>
<td>-10.6±5.3</td>
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<td></td>
<td>2.1±2.5</td>
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<td>DWBC</td>
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<td>-26.6±4.6</td>
<td>-26.5±4.1</td>
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<tr>
<td>AMOC</td>
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<td>14.3±5.2</td>
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<td></td>
<td>19.6±1.6</td>
<td>17.1±1.6</td>
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</table>
Figure 1. Geographic map showing the hydrographic sections occupied in 1992 and 2015 at 24.5° N and in 1989 and 2013 at 14.5° N. Note that only the stations with CTD profiles reaching the bottom are shown here, and that the cruise tracks at both sections are offset by 0.5 degree latitude for visual clarity.
Figure 2. The \(\theta\)-S diagram at 14.5° N (a, c) in 1989 (dark violet solid circles) and 2013 (grey open circles), and at 24.5° N (b, d) for 1992 (dark violet solid circles) and 2015 (grey open circles). The median \(\theta\)-S profiles, calculated on common neutral density grids, are shown in black for the earlier realizations at the respective sections and in light violet for the more recent realizations (cf. legend in a and b). The lower panel is the zoom of the area within the black dashed box in the corresponding upper panel. Note that the data are subsampled for visual clarity as every other profile horizontally and every 20 m vertically.
Figure 3. Vertical sections of salinity at 14.5° N in (a) 1989 and (c) 2013; and at 24.5° N in (b) 1992 and (d) 2015. Further shown is the salinity difference at (e) 14.5° N between 2013 and 1989, and (f) at 24.5° N between 2015 and 1992. Note that the difference is calculated first on neutral density levels, then transformed back onto depth levels, and that the upper 200 m are neglected. The contours in (c) and (f) are the neutral density surfaces of 27.38, 27.82, 28.072, and 28.141 kg m$^{-3}$, which marks the boundaries of AAIW, UNADW, LNADW, and AABW. The upper 1500 m in each subplot are stretched.
Figure 4. Vertical sections of potential temperature (°C) at 14.5° N in (a) 1989 and (c) 2013; and at 24.5° N in (b) 1992, (d) 2015. Further shown is the potential temperature difference at (e) 14.5° N between 2013 and 1989; and (f) 24.5° N between 2015 and 1992. Note that the difference is calculated first on neutral density levels, then transformed back to depth levels, and that the upper 200 m are neglected. The contours in (e) and (f) are the neutral density surfaces of 27.38, 27.82, 28.072, and 28.141 kg m⁻³, which marks the boundaries of AAIW, UNADW, LNADW, and AABW. The upper 1500 m in each subplot are stretched.
Figure 5. Vertical sections of oxygen (μmol kg⁻¹) at 14.5° N in (a) 1989 and (c) 2013; and at 24.5° N in (b) 1992 and (d) 2015. The "crosses" in (a) marks the position of bottle oxygen data, which are used to reconstruct the oxygen section in the western basin (see text for details). The white contour in (a) and (c) marks the 60 μmol kg⁻¹ oxygen. The upper 1500 m in each subplot are stretched.
Figure 6. Vertical sections of neutral density (kg m$^{-3}$) at 14.5° N in (a) 1989 and (c) 2013; and at 24.5° N in (b) 1992 and (d) 2015. The upper 1500 m in each subplot are stretched.
Figure 7. Initial reference velocity with error bars for the 2013 realization at 14.5° N, estimated from a combination of SADCP and LADCP (see text for details).
Figure 8. Final adjustments to the reference velocity with uncertainties along 14.5° N in (a) 1989 and (c) 2013; and along 24.5° N in (b) 1992 and (d) 2015. Note that except for the section along 14.5° N in 2013, the initial reference velocity is 0; therefore, the final adjustments in (a), (b), and (d) are equivalent to the final reference velocity.
Figure 9. The dianeutral velocity across the layer interfaces between the two sections for the periods of (a) 1989/1992 and (b) 2013/2015.
Figure 10. Final layer transports for the periods (a) 1989/1992 and (b) 2013/2015. The blue curves are the transports at the 24.5° N section including the Florida current transport, the red curves mark the transport at the 14.5° N section, the black dashed lines are the final imbalance of the layers with error bars. Note that the imbalance in each layer is calculated after taking into account the meridional and diapycnal transports across the side boundaries and vertical boundaries of that layer.
Figure 11. Meridional overturning stream function from the inverse model at (a) 14.5° N and (b) 24.5° N. It is calculated by cumulatively integrating the layer transport from the surface to the bottom. The vertical coordinate in (a) is the layer number, and in (b) the corresponding neutral density surfaces. For the 14.5° N section, the red solid curve stands for the 1989 realization, the red dashed curve for the 2013 realization. For the 24.5° N section, the blue solid curve stands for the 1992 realization, and blue dashed curve for the 2015 realization.
Figure 12. Absolute meridional geostrophic velocity along 14.5° N in (a) 1989 and (c) 2013, and along 24.5° N in (b) 1992 and (d) 2015. The station pair number is marked on the top horizontal axis. The black dashed contour line is the zero velocity contour. The black solid lines with values are the neutral density surfaces for the corresponding sections, which typically separate the thermocline water, AAIW, UNADW, LNADW, and AABW.
Figure 13. Absolute meridional geostrophic velocity in the Florida Straits in (a) 1992 and (b) 2015. The station pair number is marked on the top horizontal axis. Contour lines mark velocity in 20 cm s\(^{-1}\) interval.
Figure 4. Meridional overturning transport at 24.5° N in 2015, calculated from the inverse method (black) and RAPID array (red).
Figure 1: Meridional overturning strength at (a) 24.5° N and (b) 14.5° N, calculated from the GECCO2 (blue), RAPID (red in a), MOVE (red in b), and inverse method (black stars with error bars for the respective years). The black thick line marks the 20-month low-passed time series of the GECCO2 meridional overturning strength. Note that the MOVE time series represents the southward transport in the NADW layer (1200 to 4950 m) in the western Atlantic basin, and that the sign of the MOVE time series is artificially reversed to ease the comparison.