Effects of bottom topography on dynamics of river discharges in tidal regions: case study of twin plumes in Taiwan Strait

K. A. Korotenko¹, A. A. Osadchiev¹, P. O. Zavialov¹, R.-C. Kao², and C.-F. Ding²

¹P. P. Shirshov Institute of Oceanology, Russian Academy of Sciences, Moscow, Russia
²Tainan Hydraulics Laboratory, National Cheng-Kung University, Tainan, Taiwan

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Correspondence to: K. A. Korotenko (kkorotenko@gmail.com)
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Abstract

The Princeton Ocean Model is used to investigate the intratidal variability of currents and turbulent mixing and their impact on the characteristics and evolution of the plumes of two neighboring rivers, the Zhuoshui River and the Wu River, at the central eastern coast of Taiwan Strait. The two estuaries are located close to each other and their conditions are similar in many respects, and yet the two plumes exhibit significantly different behavior. We explain this through differences of the bottom topography in the areas adjacent to the two river mouths. The Zhuoshui River runs into a shallow area that is permanently exposed to strong tidal mixing, while the Wu River mouth is located in a deeper, stratified area outside the region of intense mixing. This destruction of the plume by tidal mixing is confirmed by the results of numerical modeling with POM. The spatial and temporal variability of turbulent kinetic energy and its production rate in the study region, as well as the horizontal diffusivity, are analyzed with the emphasis given to the dependence of the turbulence parameters on the bottom topography on the one hand and their influence on the river plumes on the other. Further, we use a Lagrangian particle tracking model in combination with POM to investigate the effect of the tidal wetting-and-drying (WAD) of land taking place near the Zhuoshui estuary, and demonstrate that WAD leads to significant reduction of the plume extent and surface salinity deficit near the river mouth. We use observational data from a short field campaign in the study area to tune and validate the model experiments.

1 Introduction

Understanding the physics of river plumes is important for predicting the pathways and fate of pollutants and other terrigenic material carried by river water. Previous studies of the topic have produced an extensive body of literature encompassing analyses of observational data (e.g., Boicourt, 1981; Münchow and Garvine, 1993; Simpson and Souza, 1995; Zavialov et al., 2003; Guo and Valle-Levinson, 2007; O’Donnell et al.,
1998; McCready et al., 2009; Jay et al., 2009; Warrick and Stevens, 2011; Kilcher et al., 2012), theoretical and numerical approaches (e.g., Chao, 1988; Oey and Mellor, 1993; Garvine, 1995, 2001; Ruddick et al., 1995; Kourafalou et al., 1996; Yankovsky and Chapman, 1997; Kasai et al., 2000; Korotenko, 2000; Valle-Levinson et al., 2003; Cushman-Roisin et al., 2007; Schiller and Kourafalou, 2010; Hwang et al., 2011), as well as laboratory experiments (Whitehead and Chapman, 1986; Avicola and Huq, 2002; Lentz and Helfrich, 2002; Horner-Devine et al., 2006; Yeping and Horner-Devine, 2013).

This article is focused on the plumes of the Zhuoshui River and the Wu River. These rivers are significant sources of freshwater discharges from the west coast of Taiwan into Taiwan Strait connecting the South China Sea and the East China Sea. While the Zhuoshui River estuary is located at a significant topographic feature called the Chang-Yuen Ridge (hereinafter CYR) and the region is characterized by a very gentle bottom slope and a considerable part of the area is subject to wetting/drying (WAD) during the tidal cycle, the Wu River runs into the ocean at the northern extremity of CYR, where the bottom slope is steeper and no significant WAD takes place. The mouths of the two rivers are situated at a distance of only 30 km from each other, the freshwater discharge rates for the two estuaries are comparable, their plumes are exposed to similar atmospheric and tidal forcing and encounter apparently similar oceanographic conditions – and yet, the two plumes exhibit significant differences in their dynamic behavior. The Zhuoshui plume is normally smaller and confined to a narrow belt along the shore, while the Wu plume tends to attain a bulge-shaped pattern and is spatially more extensive – even though the Wu River discharge rate is generally smaller than that of the Zhuoshui River. Indeed, analysis of MERIS/ENVISAT visible band satellite imagery (not shown here) since 2002 suggests that the area of the Wu River plume is larger than the area of the Zhuoshui River plume by about 40% on average.

The structure and evolution of the plume depend on a delicate balance between the input of freshwater and buoyancy from the river and plume dissipation through vertical and horizontal turbulent mixing. Hence, any model of plume evolution is particularly
sensitive to how turbulence is parameterized (Luketina and Imberger, 1989; Oey and Mellor, 1993; Ruddick et al., 1995; Garvine, 1995; Kourafalou et al., 1996; Hetland, 2005, 2010; Schiller and Kourafalou, 2010; Wang et al., 2011; Hwang et al., 2011). In this paper, we investigate the influence of mixing governed by bottom-generated turbulence on the dynamics and evolution of the Zhuoshui and Wu plumes and argue that the observed differences between the two plumes are mainly due to bottom topography. Using a high-resolution hydrodynamic model, we show that the tidal flow interacting with the CYR enhances turbulent energy production throughout the water column, thus limiting the development of the Zhuoshui River plume compared with the plume of the Wu River situated in deeper waters. Additionally, we apply a Lagrangian model to investigate the role of the tidal WAD cycle in the Zhuoshui mouth area, and show that this effect leads to further decay of the Zhuoshui plume. We use observational data from a field campaign in the study area to tune and validate the model experiments.

The article is organized as follows. Section 2 describes the study region. In Sect. 3, the field survey is described and some observational data are presented. Section 4 provides a brief overview of the two models used in this study. In Sect. 5, results of numerical simulations of the twin river plumes are given, followed by conclusions in Sect. 6.

2 Study region

Taiwan Strait (TS) connects the East China Sea in the north and the South China Sea in the south, and is sandwiched by the China mainland and Taiwan Island (Zhu et al., 2013). Figure 1 shows the bathymetry in the TS and surrounding areas. The major topographic features are the Chang-Yuen Ridge north of the Peng-Hu Channel (PHC), the Taiwan Bank (TB) in the southwestern TS, and the deepening topography in the northeastern TS. Most of the strait is shallower than 80 m. The Peng-Hu Channel is located between the Peng-Hu Archipelago and Taiwan Island, descending southward sharply from 70 m to deeper than 1000 m. It is generally believed that the Peng-Hu
Channel is important in conducting the water from the southern opening of Taiwan Strait into the rest of the strait (Chuang, 1985, 1986; Wang and Chern, 1992; Jan et al., 1994). In this study, we focus on the CYR region. In the central TS, the tidal flow impinging on the CYR is separated so that the surface and bottom waters flow in different directions: heavier deep waters separate from the Taiwan coast south of the CYR, while lighter surface waters flow over the CYR and spread along the eastern coast of the TS (Jan et al., 1994). The general flow in TS is represented by the northeastward Taiwan Current, which is a coastal branch of the Kuroshio Current flowing north along the continental slope east of Taiwan.

A crucial role in the circulation of TS is played by semidiurnal tidal oscillations (Chuang, 1985, 1986; Jan et al., 2002). Generally, it is believed that the tide penetrates into Taiwan Strait through the northern and the southern openings, then converging in the central part of the strait. Lin et al. (2000) argued that the semidiurnal tide in Taiwan Strait is represented as a standing wave, while Jan et al. (2002) suggested that the propagating and standing semidiurnal tides coexist, with most of the energy of the semidiurnal tide coming from the north. The diurnal tide in Taiwan Strait is less intense than the semidiurnal tide, except in the southernmost sector. Sea level measurements revealed that the diurnal tide propagates from north to south (Hwung et al., 1986).

Another important oceanographic feature in the TS is massive discharge of fresh water from multiple rivers. With its length of 176 km, catchment area of 3160 km² and long-term average discharge rate of 210 m³ s⁻¹, the Zhuoshui River is the largest of those at the western coast of Taiwan. The Zhuoshui River’s region of freshwater influence (ROFI) stretches along the western coast. In the north, it often merges with the ROFI of the Wu River (also known as the Dudu River) whose average discharge rate is about 120 m³ s⁻¹.
3 Field data

A map of the field survey conducted on 25–27 June 2013, is shown in Fig. 2. A local fishery boat was used to take measurements at 13 hydrographic stations in the coastal zone. All stations were occupied on 27 June.

Temperature and salinity along the ship’s track were recorded continuously using a pump-through CTD system. In addition, at each of the stations, surface-to-bottom CTD profiling was conducted and water samples were collected from the surface and the near-bottom layer. Standard Sea Bird’s SBE19plus instruments were used for the profiling and in the pump-through device.

The water velocity was continuously measured at a single point as 10 min averages by SeaHorse mechanical current meter (Sheremet, 2010) during 25–27 June. The instrument was deployed at a depth of about 5 m at a distance of 4 km to the west from the Zhuoshui River estuary (23.8488° N, 120.1995° E).

A portable meteorological station was mounted at a height of about 10 m above the sea level at the top of an old lighthouse at the Wu River mouth, 32 km north of the Zhuoshui River estuary. The station started working at 10:00 GMT, 25 June, and the data of wind speed and direction, as well as atmospheric pressure, air temperature and humidity were collected as 20 min averages until 23:30 GMT, 28 June.

As can be observed in Fig. 2, during the survey, the Zhuoshui River plume was manifested as a belt of low salinity (below 30 psu) oriented along the coast in a pattern suggesting northward propagation. Yet fresher water (S < 25 psu) is seen in the area adjacent to the river mouth, where the inner part of plume forms a sharp salinity front approximately at the 5 m isobaths. The velocity record for 25–27 June as obtained by the current meter is shown in Fig. 3 (lower panel), indicating dominance of semidiurnal tides.
4 Models

To investigate the dynamics of the Zhuoshui River and Wu River plumes, hereinafter we use two numerical models, namely, the well-known a finite difference, $\sigma$ coordinate Princeton Ocean Model (POM), and the recently developed Lagrangian model STRiPE (Osadchiev and Zavialov, 2013). The two models complement each other for simulating the complex dynamics of the plume.

4.1 Implementing POM

The POM is a 3-D primitive equation ocean model that includes full thermodynamics and a level 2.5 Mellor–Yamada turbulence closure (Blumberg and Mellor, 1987; Mellor and Yamada, 1998). The POM model grid area covers the middle part of Taiwan Strait from 116.5° E to 121.0° E and from 23° N to 25° N (Fig. 4). The model domain is divided into 270 $\times$ 122 grid cells whose sizes $\Delta x$ in longitudinal direction and $\Delta y$ in latitudinal direction are both equal to one nautical minute. This corresponds to zonal resolution ranging from 1.723 km at 23° N to 1.698 km at 25° N, and meridional resolution of 1.836 km. In the vertical, 21 $\sigma$ levels are unevenly distributed, so that higher resolution is set to be near the surface and bottom. The minimum water depth in the model domain was set to 4 m.

The time steps were set to 3 s for the external mode and 120 s for the internal mode. The vertical eddy viscosity and diffusivity were provided by the Mellor–Yamada turbulence closure scheme with a background value of $10^{-5}$ m$^2$s$^{-1}$. The horizontal eddy viscosity, $A_L$, was calculated through the embedded Smagorinsky formula

$$A_L = C_H \Delta x \Delta y \sqrt{\left(\frac{\partial u}{\partial x}\right)^2 + \left(\frac{\partial v}{\partial y}\right)^2 + \frac{1}{2} \left(\frac{\partial u}{\partial y} + \frac{\partial v}{\partial x}\right)^2},$$

(1)

with a proportionality parameter, $C_H$, equal to 0.1, and the horizontal eddy diffusivity, $K_L$ was obtained based on the inverse Prandtl number of 0.5.

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The model was forced with tides and river discharge. The river input was imposed at the corresponding grid points by specifying the vertical velocity at the sea surface, \( w_S \). Following Oey (1996), we specify it as

\[
    w_S = -Q/(N \Delta x \Delta y),
\]

where \( Q \) is river discharge rate (m\(^3\) s\(^{-1}\)), \( N \) is the number of grid areas around the river mouth where the discharge is to be distributed. We assume that \( w_S \) injects volume and freshwater, (salinity = 0 psu) but no momentum.

One important feature of the region of our interest is the CYR which may significantly affect the structure of the along-shore flow and enhance tidal mixing as the current impinges on the ridge. To describe this effect, it is important to adequately simulate the bottom stress. In the POM, the stress, \( \tau_x^b \) and \( \tau_y^b \) induced by the bottom friction is described as

\[
    \left( \tau_x^b, \tau_y^b \right) = C_z \left( u^2 + v^2 \right)^{1/2} (u, v),
\]

where \( u \) and \( v \) are the horizontal velocity components and \( C_z \) is the non-dimensional coefficient, which is a function of the roughness length of the bed, \( z_0 \), and the water depth, \( H \)

\[
    C_z = \text{MAX} \left( \frac{\kappa^2}{\ln\left( (1 + \sigma_{kb-1})H/z_0 \right)^2}, 0.0025 \right)
\]

where \( \kappa = 0.4 \) is the von Karman constant, \( \sigma_{kb-1} \) is the depth of the layer overlying the bottom one in sigma coordinates. In other words a logarithmic current profile is assumed and the bottom friction is determined by the current velocity of the layer nearest to the bed.

For stability of numerical simulations of flows in shallow regions, such as straits and channels, the Manning formula for bottom friction is often applied (e.g., Liu at al., 2003;
Chiou et al., 2010). Instead of Eq. (4) we use the following formula for the coefficient $C_z$:

$$C_z = \frac{g}{C^2}$$

(5)

where $C = n^{-1}H^{1/6}$, $n$ is the Manning coefficient and $g$ is the acceleration of gravity. The bottom friction is determined with a use of the vertical mean of $u$ and $v$ in Eq. (3) at the corresponding location. In this case, therefore, the velocity is much less sensitive to the logarithmic profile assumption used in conventional parameterizations for $C_z$ which may lead to large errors and spurious features over steep topography. Following Chiou et al. (2010), for Taiwan Strait, we set the Manning coefficient $n$ to $0.032 \text{ s m}^{-1/3}$.

At the open (northern, $N_b$ and southern, $S_b$, see Fig. 4) boundaries of the model domain, two types of boundary conditions for the temperature and salinity were used, namely, the condition for inflow and that for outflow. In the case of the inflow into the domain, the values for $T$ and $S$ at the corresponding open boundary were accepted. In the case of the outflow from the domain, the radiation condition

$$\partial_t (T, S) + U_n \frac{\partial}{\partial n} (T, S) = 0,$$

(6)

was used, where the index $n$ represented the direction normal to the open boundary.

The barotropic (vertically averaged) velocities on the open boundaries of the POM were estimated using the Flather (1976) formula:

$$\bar{u}_n = \bar{u}_n^0 + \sqrt{\frac{g}{H}}(\eta - \eta_0),$$

(7)

where $\bar{u}_n^0$ and $\eta_0$ are the vertically averaged normal component of the velocity and sea surface elevation at open boundary, respectively, from the barotropic tidal model of Hu et al. (2010); $\bar{u}_n$ is the vertically averaged normal component of the velocity at the open
boundary at time $t$; $\eta$ is the model sea surface elevation calculated from the continuity equation and located half a grid cell inside of the open boundary in the POM model domain.

The tidal model data used corresponded to the period of our field survey mentioned above, i.e., 25–27 June 2013. Figure 3 illustrates current velocities obtained from the POM forced by tide and the northeasterly wind of 5 m s$^{-1}$ vs. the measurements conducted with SeaHorse current meter on 25–27 June 2013. Despite diurnal variations of wind, the comparison shows a reasonably good agreement between tidal variations of the modeled and measured velocities, except perhaps a discrepancy from about 00:00 to 06:00 GMT on 27 June, presumably caused by an advective event.

In the experiments described in the rest of this article, we run POM under the tidal forcing only, with no wind forcing.

4.2 Implementing the STRiPE model

The STRiPE (Surface-Trapped River Plume Evolution) is a recently developed Lagrangian numerical model designed specifically for simulating river plumes under various forcing conditions. Detailed description of the STRiPE model, as well as its validation and examples of its application to river plumes, are given in (Osadchiev and Zavialov, 2013). The STRiPE model tracks the motion of river water “particles” discharged into the sea. The particles are the elementary water columns released from the river mouth, assigned with the initial velocity depending on discharge rate. The initial height, density, and salinity of the particles are set equal to river mouth depth, density, and salinity. While moving, the particles are allowed to mix with the seawater, so their characteristics change in time. Finally they become equal to the characteristics of the ambient ocean, in particular, particle height becomes equal to zero that means that the particle eventually dissipates. In the model, vertical mixing is based on the
Salinity diffusion equation:
\[
\frac{\partial S}{\partial t} = D_v \frac{\partial^2 S}{\partial z^2},
\]
where \( S \) is particle salinity, and \( D_v \) is the vertical diffusion coefficient parameterized via the Richardson number \( R_i \) and scaling coefficient \( C_v \) as given in Large (1994):
\[
D_v = C_v (1 - \min(1, R_i^2))^3.
\]

Considering the main forces that determine river plume dynamics, namely, the Coriolis force, the force applied from the wind, the friction with the underlayer flow, the lateral friction, and the pressure gradient force, the model then solves the momentum equations applied to the individual particles. Small-scale horizontal turbulent mixing is modeled by the random-walk method (Hunter, 1987) complementing the momentum equations. Horizontal turbulent diffusivity \( K_L \) used in the random-walk scheme is parameterized by the Smagorinsky diffusion formula (Eq. 1). At every step of the model integration, the overall set of particles represents the river plume, and hence the temporal evolution of the plume structure is obtained.

The advantage of the STRiPE consists in computational efficiency and relative easiness of simulating a variety of aspects of plume dynamics. Here, we use it to elucidate the role of WAD effects. However, a significant drawback of the model lies in the fact that the circulation of oceanic waters, surrounding the river plume, cannot be simulated by the STRiPE model itself. The background velocity field must be prescribed as input data, obtained either from measurements or from another model. We, therefore, use the STRiPE in combination with POM.

The STRiPE was applied to the study region, including the WAD zone (about 4 km wide) near the Zhuoshui River estuary. The behavior of the Zhuoshui River and the Wu River plumes was simulated under 3 different wind regimes, namely, no wind, NE, and SW, as the wind conditions most common for the study region (Liu et al., 2009). The numerical experiments were set up as follows. The model domain was the area...
between the Zhuoshui and Wu estuaries with the realistic shoreline from 120.0° E to 120.65° E and from 23.7° N to 24.5° N. The freshwater particles were released from the Zhuoshui River and the Wu River estuaries with the initial velocities of 0.1 ms\(^{-1}\). The initial vertical scale of the released water volumes (i.e., the plume thickness at the mouth) was assumed equal to 5 m. The model integration time step was set to 10 min, while the total simulation period was 2 days, from 01:00 GMT of 26 June 2013, through 01:00 GMT of 28 June 2013. For diagnostic experiments with the constant NE and SW winds, the wind speed was set equal to 5 ms\(^{-1}\). The input data of the ambient velocity fields were imported from the POM simulations.

5 Results and discussion

5.1 Vertical structure of tidal velocity

Figure 5 shows the simulated sea surface height (SSH) and the velocity components at both selected sites near the Wu River (Site 1) and Zhuoshui River (Site 2) mouths. It can be seen from the figure that the along- and cross-shore components of the velocity were tidally forced and exhibited semidiurnal variability. The zonal (cross-shore) velocity at Site 1 exceeded 0.55 ms\(^{-1}\) for the flood flow and flow \(-0.44\) ms\(^{-1}\) for the ebb, while the meridional (along-shore) velocity component was somewhat smaller during both flood and ebb. For the study area, a flood phase of tide occurs when flow turns to the northeast and ebb phase occurs when flow turns to the southeast. A peculiar feature of tidal dynamics in this area is the asymmetry of the SSH curve and current velocity, so that near the Wu River (Site 1), the period of falling tide lasted less (\(\sim 1\) h) than that of the rising tide. Note that here, the flood and ebb peaks perfectly coincide with maximum and minimum of the SSH, respectively. The water slacks occur at the middle of the transition period between the flood and ebb tides. In contrast, a stronger shift between the SSH curve and the tidal current takes place at shallower Site 2 (Zhuoshui River), where the ratio between the falling and the rising tides is the same as above, but
the tidal current velocity leads the maximum of SSH by approximately 1.5 h. At the Site 2, the meridional velocity, on the flood flow, exceeded 1.2 m s\(^{-1}\) and \(-1.1\) m s\(^{-1}\) on the ebb flow, while the zonal velocity component was weaker and its magnitude was below 0.6 m s\(^{-1}\). The slight slope of the velocity contours in Fig. 5 suggests that the tidal currents at a surface lag those in the near-bottom layer. This is clearly seen at Site 1 near the Wu River mouth. At the shallower Site 2 tidal mixing partly offsets this effect. It can also be seen from Fig. 6 that the slacks when velocity falls to zero, and the moments of current reversal for the Zhuoshui River area precede those for the Wu River. Such an “asymmetry” may result in periodic mergers and separations of the plumes during the tidal cycle.

5.2 Horizontal structure of tidal currents and evolution of the river plumes

In the numerical experiments described in what follows, the discharge rates for both rivers were set to 210 m\(^3\) s\(^{-1}\), which is the climatic average for the Zhuoshui River. As a matter of fact, the long-term average discharge rate of the Wu River is somewhat lower, but the runoffs are highly variable in time, and for the purposes of this study we set the discharges of both rivers equal to each other in order to emphasize other dynamical factors determining differences in the behavior of the two plumes. To reach the stabilization of plume sizes, tidal forcing was applied as a seamless perpetual 3 day cycle from 25 to 27 June 2013 – each run started on 25 June from the first water slack event following the ebb, and stopped with the second slack at the end of 27 June. With the chosen discharge rate values, the stabilization of plumes was attained during 3 × 3 computational days.

Figure 6 shows four successive phases of the tidal velocity and the respective Zhuoshui River and Wu River plumes as obtained for 27 June. The velocity fields and the plumes are presented against the position of the 30 m isobath, which approximately delineates the Chang-Yuen Ridge plateau. The tidal cycle was mostly governed by the semi-diurnal M2-constituent with a period of approximately 12.4 h. Figure 6b and d clearly illustrate significant enhancement of the flood and ebb flows over the CYR.
Here, the velocity peaks exceeded 1.2 m s\(^{-1}\) and –0.8 m s\(^{-1}\) during the flood and the ebb, respectively. The 30 m isobath helps to determine the mean position of the flow-enhanced area above the CYR during the tidal cycle. However, in the flood phase, this area is notably shifted to the north with respect to the 30 m isobaths (Fig. 6b), while during the ebb the flow-enhanced area is shifted to the south (Fig. 6d).

The numerical experiments highlighted important differences evident in the shape and the behavior of the two plumes. Although the discharge rates of the Zhuoshui River and the Wu River were set equal, throughout the tidal cycle, the Zhuoshui River plume was somewhat narrower, and less regularly shaped and more eroded than the Wu River plume. The latter attained a “classical” bulge-like shape, which remained well pronounced, albeit its position shifted back and forth with the tidal oscillations. In contrast, the Zhuoshui River plume stretching along the shore as that of the Wu River but its shape is largely distorted by turbulent mixing.

Such differences in the structure and the evolution of the two plumes located so close to each other are likely to be associated with inhomogeneous structure of turbulence caused by the interaction of tidal flow with the bottom topography. In particular, the shallow CYR must play a central role in such interaction. In the next subsection, we use the so-called Simpson–Hunter parameter (Simpson and Hunter, 1974) to elucidate this effect. This parameter allows approximating identification of the limit between tidally well-mixed and stratified zones. Furthermore, we focus on the tidally well-mixed zones near the CYR and the river plumes.

5.3 The Simpson–Hunter parameter

Using simple energy budget considerations, Simpson and Hunter (1974) argued that the location of the frontal zone between tidally well-mixed and stratified regions – including those formed by river discharges – can be estimated by a critical value of the tidal mixing parameter \(K_{\text{SH}}\):

\[
K_{\text{SH}} = \log_{10}(h/u^3),
\]

(10)
where \( h \) is the mean water depth (m), and \( u \) is the depth-averaged tidal velocity (m s\(^{-1}\)). The value of \( K_{\text{SH}} \) essentially reflects the mean intensity of tidal mixing through the water column at a specific location. As \( K_{\text{SH}} \) decreases, either because the water depth \( h \) decreases or the tidal current \( u \) increases, the tidal mixing becomes stronger, and vice versa. This approach has been successfully applied to investigating tidal fronts on the continental shelves in a number of more recent studies (e.g., Zhao, 1985; Garrett and Maas, 1993; Hu et al., 2003; Lü et al., 2007; Holt and Umlauf, 2008; Zhu et al., 2013). For Taiwan Strait, the critical value of the parameter, as was found by Zhu et al., 2013, is equal to \( K_{\text{SHc}} = 1.78 \). Note that the Simpson–Hunter parameter was originally proposed for thermal stratification resulting from solar radiation producing buoyancy in the surface layer. In present work, we extend this approach to include lateral contrasts of buoyancy due to river discharges.

We computed the distribution of \( K_{\text{SH}} \) using the velocity obtained from the POM. Figure 7 (left panel) exhibits the contours where the parameter \( K_{\text{SH}} \) attains this critical value of 1.78, for the study region during the flood flow. As seen, the critical contour of \( K_{\text{SH}} \) delineates the CYR, indicating that strong tidal mixing occurs over the entire CYR. For comparison, in the right panel of Fig. 7 we present the critical tidal mixing parameter, \( K_{\text{SHc}} \), for the entire TS estimated from CTD measurements during the eight years (2004–2011) by Zhu et al. (2013). These estimates also indicate strong tidal mixing in the area over the CYR in the vicinity of the Zhuoshui and Wu Rivers.

As Fig. 7 (right panel) shows, the Zhuoshui River mouth is inside the critical \( K_{\text{SH}} \) contour, while the Wu River estuary is outside it. This fact may explain the differences in the behavior of the plumes during a tidal cycle: the Zhuoshui River discharges the river water into the zone of intense tidal mixing, therefore, the plume is exposed to extreme erosion. In contrast, the Wu River delivers river water into a moderate mixing zone, a few miles north from the CYR energetic zone as indicated by the critical \( K_{\text{SH}} \) contour in Fig. 7, although the ebb phase of the tide advects the river water southwestward towards the enhanced mixing zone. This results in narrowing of the southern extremity of the Wu River plume, evident in Fig. 6d. However, during the entire tidal cycle, most
of the Wu River plume lies outside of the intense tidal mixing zone, which may explain the relatively weak destructive effect of mixing on its bulge (Fig. 6a–d).

Thus, the Simpson–Hunter parameter is useful for determining of tidal mixing zones and qualitative elucidation of their potential effect on the fate of the river plumes. However, more in-depth analysis requires more information on turbulent structure in the study region. In the next subsections, we analyze some modeled turbulent parameters, giving emphasis to the features that may help to explain the differences in the characteristics of the Zhuoshui River and the Wu River plumes.

5.4 Turbulent kinetic energy production rate

In the bottom layer of the ocean, the water flowing above the seabed experiences frictional stress, which extends upwards throughout the water column. The bottom friction is one of the major causes of tidal turbulent kinetic energy (TKE) production in shallow water. The stress due to bottom friction is (Tennekes and Lumley, 1972):

\[ \tau_b = C_D \rho u |u|, \]  

where \( C_D \) is the drag coefficient, \( \rho \) is the sea water density, and \( u \) is the current velocity. It follows then that the work \( A \) done by the bottom stress per unit time is expressed as:

\[ A = C_D \rho |u|^2 u^2, \]  

where \( A \) is assumed to balance the energy dissipation that occurs in the boundary layer (although this is not the case for non-equilibrium turbulent regimes, as shown by direct measurements of turbulence with ADCP in energetic tidal channels and estuaries, e.g., Rippeth et al., 2002; Williams and Simpson, 2002; Korotenko et al., 2012, 2013). As the tidal current flows across the shoal of small depth, the current velocity increases due to the conservation of mass. TKE production and dissipation rates will, therefore, grow as the third power of the current speed.
As was mentioned above, the CYR plays a significant role in enhancing the tidal currents and, hence, TKE production in the bottom boundary layer. The upward-propagating turbulence generated by the tidally oscillating bottom stress, in shallow areas, can mix the entire water column and, thus, affects intertidal river plume dynamics.

Figure 8 shows horizontal distributions of the computed TKE production rate at 1 m depth for two phases of tide, namely, the water slack at 08:00 GMT and the peak flood at 11:00 GMT on 27 June 2013. It can be seen that high levels of TKE production rate occur mainly above the CYR, where its value exceeds $10^{-3}$ Wm$^{-3}$ during the flood.

As already illustrated by the Simpson–Hunter parameter above, the TKE production distributions shown in Fig. 8 indicate that the continental waters discharged from the Zhuoshui River and the Wu River propagate in energetically different ambiances: while the Zhuoshui River plume spreads through high TKE production area over the CYR and is, therefore, subject to faster erosion, the Wu Rivers plume spreads mainly in a “calm” area of moderate TKE production, retaining larger area and the classical shape of the plume (Yankovsky and Chapman, 1997).

5.5 Zonal transect of TKE production rate

River plumes are not only passively destroyed by turbulent mixing – in turn, they tend to damp turbulence because of buoyancy inflow. To demonstrate this effect, in Fig. 9, we present the flood phase zonal transect of TKE production rate along 24.2° N, i.e., along the northern edge of the CYR to the Wu River mouth. As the distribution of TKE production rate indicates, the energy of bottom-generated turbulence generally decreases upwards. The most obvious consequence of the freshwater input in mixing water is suppressing turbulence in a localized zone adjacent to the coast and corresponding to the Wu River plume (Fig. 9).

Figure 9 also demonstrates that the Wu River plume consisted of the nearshore part and the offshore part, separated by a tongue of highly energetic turbulence generated near the ascending bottom. Note that offshore plume belongs to so-called
surface-advected type of the river plume, according to classification by Yankovsky and Chapman (1997). Inside the plume, TKE production rate fell below $10^{-6} \, \text{W m}^{-3}$, indicating significant suppression of turbulence by buoyancy (even in the strong flood phase).

The zonal vertical distribution of TKE production along a similar transect near the Zhuoshui River mouth (not shown) resembles that for the Wu River, although the plume of the Zhuoshui River is notably narrower.

### 5.6 Time-depth variability of turbulent parameters

#### 5.6.1 TKE

Generally, in tidal flows, variations of turbulent kinetic energy are tightly connected with the tidal cycle (e.g., Rippeth et al., 2003; Souza and Howarth, 2005; Wiles et al., 2006; Korotenko et al., 2012, 2013). The simulated time series of the vertical structure at TKE for Sites 1 and 2 are depicted in Fig. 10. During the tidal cycle, the TKE spans about four orders of magnitude. During the tidal slack, the TKE sharply drops below $10^{-4} \, \text{m}^2 \text{s}^{-2}$ throughout the water column. The TKE attains a maximum in the bottom layer and decreases upwards. The most important finding illustrated by Fig. 10 is the following: while in the Zhuoshui River plume area (lower panel), TKE values above $10^{-3} \, \text{m}^2 \text{s}^{-2}$ emerge at the surface because of shallower water and higher velocity, in the Wu River plume area (upper panel), the penetration of TKE generated by the bottom stress is limited to about 25 m above the bottom and, hence, does not reach the surface layer. This supports the central hypothesis of this article: the dynamic behaviors of the Zhuoshui and Wu plumes are different because their evolution occurs under different regimes of turbulent mixing.

#### 5.6.2 Horizontal diffusivity, $K_L$

The discussion above was focused on the vertical turbulent mixing in connection with the bottom topography. However, horizontal mixing can also contribute significantly to
the evolution of the plumes. For example, Kourafalou et al. (1996) studied the effect of variability of the horizontal diffusivity on the development and dynamics of a river plume and found that, as the horizontal diffusivity decreased, the along-shore and cross-shore dimensions of the river plume increased while coastal current meandering diminished. Their experiments were performed with constant values of $K_L$, which may be appropriate for experiments with a stable external forcing. However, in reality, the plume dynamics is more complex and the impact of variable horizontal diffusivity on river plume dynamics should be taken into account. Therefore, in this paper, we examine the time-depth variability of the $K_L$ (Eq. 1) over the tidal cycle.

Figure 11 exhibits the time-depth variability of the horizontal diffusivity at Sites 1 and 2. Comparing the variations of $K_L$ at the two sites, we can see considerable differences that are likely to be caused by the flow impinging on the CYR. The influence of the ridge significantly affects the velocity field deformation. As Fig. 11 indicates, for the Site 1 near the Wu River during the flood, the maximum of $K_L$ occurs at the sea surface, while during the ebb it migrates to the intermediate depths of 5–10 m. Figure 6b and c above demonstrate some widening of Wu River’s plume north of the mouth, which may be an evidence of the contribution of horizontal diffusion to spreading of the plume during the flood phase. In contrast, at Site 2 near the Zhuoshui River, the horizontal diffusivity significantly increased during the ebb, i.e., velocity deformation peaked when the sea surface height over the CYR attained its minimum. Thus, comparing the variability of $K_L$ near the Wu River and Zhuoshui River, we again found considerable differences, potentially important for the dynamics of the river plumes.

### 5.7 The role of WAD

In terms of the tidal wetting and drying (WAD), the areas adjacent to the Zhuoshui River and the Wu River exhibit very different conditions. The shallow and flat bottom near the Zhuoshui River mouth dries during the low tide phase in a vast, about 15 km long and 4 km wide segment of the coastline (Fig. 12), while the deeper shelf near the Wu River mouth has no significant WAD and constantly remains covered with water.
This feature gives us an opportunity to investigate the influence of WAD processes on river plume dynamics. Because the version of POM used in this study was not intended to simulate WAD, for this purpose we used the Lagrangian model STRiPE. The model and the experimental setup are described above in Sect. 4.3.

Firstly, we simulated the behavior of the Zhuoshui River and the Wu River plumes with the fixed shoreline corresponding to the high tide phase of the WAD cycle. Secondly, we ran the model with the WAD cycle and the movement of the boundary taken into account. The movement of the shoreline between its highest and lowest tide positions was set uniform for every tidal cycle. We performed two POM simulations, one with the high tide shoreline and the other one with the low tide shoreline configurations (outside the WAD region, the shelf circulations obtained for the two cases exhibited only minor differences). If there was no WAD area at the model domain, the set of intermediate velocity fields between high and low tide phases could be computed as transitional averages between the two limiting cases. In presence of WAD these average velocity fields should be additionally resized in accordance with the contraction of the field domain caused by uniform movement of the shoreline in the WAD region. The resulting set of fields is used as an input for the STRiPE simulation. The boundary condition for the STRiPE in the WAD zone was no-normal flow at the coastline, i.e., once the “particle” hits the shoreline, the cross-shore velocity of the “particle” is set equal to the shoreline, while the along-shore velocity component retains its value without change. Both STRiPE simulations (with and without WAD) were performed without wind forcing, and the ambient sea circulation was adapted from the POM experiments as described above. Comparing the results of the two simulations, we can obtain some insights into the role of WAD. In Fig. 13, we present the modeled surface salinity distributions outside the WAD region averaged over 48 h simulation period, namely, from 01:00 GMT of 26 June 2013, through 01:00 GMT of 28 June 2013.

It can be seen from Fig. 13 that the presence of WAD significantly changed the Zhuoshui River plume at the WAD zone; plume area decreased considerably compared with the “no WAD” conditions. The salinity anomaly in the plume also decreased by
about 3 psu. At the same time, the Wu River plume was affected less significantly. Hence, it is likely that WAD adds significantly to the erosion of the Zhuoshui River plume. The possible physical mechanism is as follows: the emergence of a piece of land during the low tide phase alters the along-shore current on the inner shelf and increases shears, which, in turn, enhances mixing down through the water column in the plume area.

6 Summary and conclusions

A high-resolution Princeton Ocean Model was used to investigate the intratidal variability of currents and turbulent mixing and their impact on the characteristics and evolution of the plumes of two neighboring rivers, the Zhuoshui River and the Wu River, at the central eastern coast of Taiwan Strait, where the shallow sand Chang-Yuen Ridge is a significant feature of the bottom topography having considerable impacts on the local dynamics. The two estuaries are located close to each other and the conditions they are exposed to are similar in some respects, and yet the two plumes exhibit significantly different behavior. We attribute this to the differences in the bottom topography. Indeed, as numerical experiments showed, the Wu River plume located in a relatively deep area at the northern extremity of the CYR is characterized by larger spatial extent and tends to maintain its “bulge-like” shape throughout the tidal cycle, whilst the Zhuoshui River plume localized over shallow and flat bottom terrain is reduced in size, stretched along the shore and eroded by turbulent mixing.

We applied the Simpson–Hunter criterion (Simpson and Hunter, 1974) to qualitatively explain the differences between the two plumes, and found out that, according to the criterion, the Zhuoshui River runs into the area that is permanently well mixed, and the Wu River mouth is located in a stratified area outside the region of intense tidal mixing. This is also confirmed by the results of numerical modeling with POM. It was demonstrated that the area of bottom-generated turbulence, which is strong during the ebb and flood flows, coincided with the shallow area above the CYR, thus indicating
a dissimilarity of tidal mixing acting on the two plumes. The turbulent kinetic energy production rate was found to vary strongly, attaining maximum values of about $10^{-1}$ W m$^{-3}$ over the CYR at the seabed during the flood and ebb tide. Away from the bottom layer, the TKE production gradually decreased upwards and was significantly suppressed in the surface layer by strong stratification generated by the river plumes. Inside the plumes, TKE production rate fell below $10^{-6}$ W m$^{-3}$.

Further, we analyzed the time-depth variability of TKE. The predicted bottom-stress-generated TKE was found to vary by 4 orders of magnitude. Near the Zhuoshui River mouth the bottom-generated turbulence penetrated throughout the water column and reached the sea surface during the ebb and flood tide phases, significantly mixing and eroding the river plume. On the other hand, in the deeper area near the Wu River plume, the bottom-generated TKE was not strong enough to mix the water column up to the surface and had only marginal influence on the plume.

Horizontal turbulent mixing also contributes to the plume dynamics and demonstrated certain dissimilarities for the two river plumes. In the Zhuoshui River area during the flood, the maximum of horizontal diffusivity occurred at the surface, while during the ebb it moves to intermediate depths below the plume layer. In contrast, in the Wu River mouth area the horizontal mixing was generally smaller and attained a maximum during the ebb phase throughout the water column.

In addition, we applied a Lagrangian particle-tracking model used in combination with POM to investigate the effect of tidal wetting-and-drying of the land near the Zhuoshui River mouth. It was found that this process adds to downward mixing of the Zhuoshui River plume.

Altogether, these findings point on extreme importance of bottom topography features for the dynamics of river discharges in tidal regions.

In conclusion, it should be noted that the environments of both rivers have been seriously threatened in recent years by ongoing construction activities, concrete industry and agriculture. Particularly, the concentration of metals such as copper and iron was elevated over the regulated standard. The elevated level of copper was attributed to
the addition of that in the animal feeds for many livestock in the area (Environmental Policy Monthly, 2010). Thus the present study is certain to be important in understanding fate and distribution of various contaminants delivered into marine environment by the Zhuoshui and Wu Rivers.

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Fig. 1. Bathymetry of Taiwan Strait. TB is Taiwan Bank, PH is Peng-Hu Archipelago, CYR is the Chang-Yuen Ridge, PHC is the Peng-Hu Channel. Points 1 and 2 indicate the locations of the sites we refer to in the discussion. The mean water depths at sites 1 and 2 are 33 m and 13 m, respectively. Modified from Jan and Chao (2003).
Fig. 2. Left: bathymetry of the Zhuoshui mouth area (based on ETOPO1). The isobaths are labeled in m. Right: map of stations occupied during the field survey in June 2013 (bullets). Black box indicates the position of mooring station with current meter near the bottom. Black curves are the estimated surface salinity contours (morning of 27 June).
Fig. 3. Lower panel: hourly averaged vectors of the current velocity at the depth 5 m obtained at the mooring station. Middle panel: same series as simulated by POM model, see Sect. 3. Upper panel: series of wind velocity as measured for the same period.
Fig. 4. The POM domain and bottom topography. Locations of Zhuoshui River and Wu River mouths are indicated by white dots.
Fig. 5. Time-depth variability of the sea surface height, zonal (eastward direction is positive) and meridional (northward direction is positive) tidal velocities at Site 1 (upper panels) and Site 2 (lower panels).
**Fig. 6.** Successive phases of tidal velocity and salinity at 1 m depth at (a) 08:00, (b) 11:00, (c) 14:00, and (d) 17:00 GMT on 27 June 2013. The phases (b and d) correspond to the peak flood (northeastward) and ebb (southwestward) flows, respectively. The 30 m isobath (solid blue line) approximately delineates the Chang-Yuen Ridge. The 32.5 psu salinity contour delineates the river plumes.
Fig. 7. Left panel: planar plot of computed SH parameter in the coastal zone over the CYR area including Zhuoshiu and Wu Rivers’ mouths. The contour of $K_{SHc} = 1.78$ (red line) and isobath of 30 m delineating the CYR (white line) are shown. The modeled $K_{SH}$ corresponds to flood phase at 11:00 GMT, 27 June 2013. Right panel: MODIS images of Chl $a$ on 9 July 2009. The contours for the critical tidal mixing parameter ($K_{SHc} = 1.78$) estimated from CTD measurements by Zhu et al. (2013) are shown in red. Locations of the summertime upwelling cores in the TS are shown with blue ellipses. Acronyms are given in Fig. 1.
Fig. 8. Modeled horizontal distributions of TKE production rate at 1 m depth at (a) 08:00 and (b) 11:00 GMT on 27 June 2013.
Fig. 9. Zonal vertical distribution of TKE production rate over the CYR along 24.2°N at 11:00 GMT on 27 June 2013. Flood phase.
Fig. 10. Modeled time–depth variability of TKE at Site 1 (Wu River area) and Site 2 (Zhuoshui River area). The ordinate axis is height (m) above the bottom, mab. Ocean surface elevation is depicted by black line.

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Fig. 11. Simulated time-depth variability of horizontal diffusivity, $K_L$, at Site 1 (Wu River area, upper panel) and Site 2 (Zhuoshui River area, lower panel).
Fig. 12. Model domain for numerical simulations with STRiPE. Also shown are the shorelines for low tide (yellow) and high tide (red) conditions. The area between the red and the yellow contours is the WAD region.
Fig. 13. Modeled surface salinity distributions at the study area without WAD (left) and with WAD (right) under “no wind” conditions averaged for the period from 01:00 GMT of 26 June 2013, through 01:00 GMT of 28 June 2013.